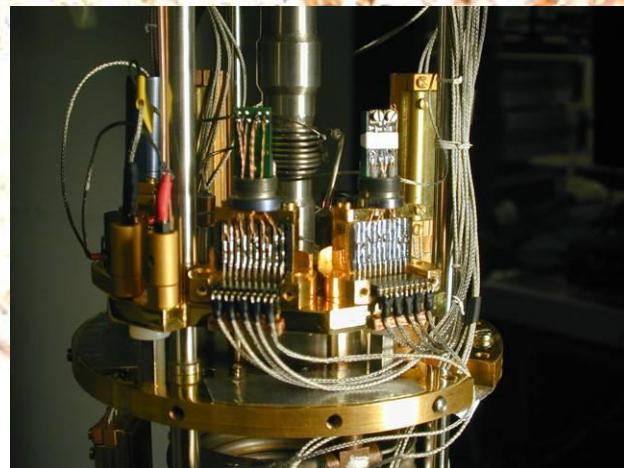
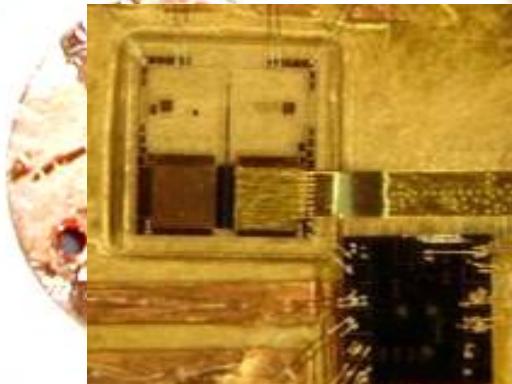
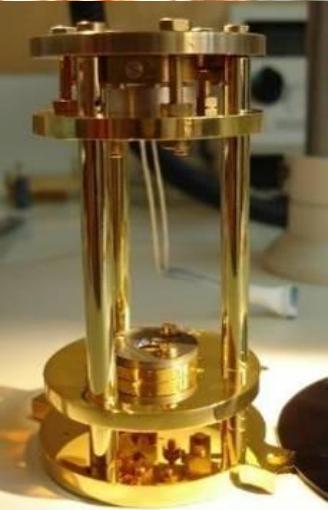


# Metallic Magnetic Calorimeters for spectrometry applications

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DRTBT09 : 6ième école thématique  
Perspectives des détecteurs cryogéniques



# Metallic magnetic calorimeter

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- Physical principle
  - Choice of the paramagnetic sensor
  - The calculation of signal size
  - Intrinsic sources of noise
- Detector read out
  - SQUID read out and performances
  - SQUID-detector coupling
- Optimizations
  - Signal to noise ratio
  - Fabrication and experimental set-up

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- Applications

- External sources

- X ray spectrometry

- Gamma ray spectrometry

- Embedded source in the detector

- Activity measurement

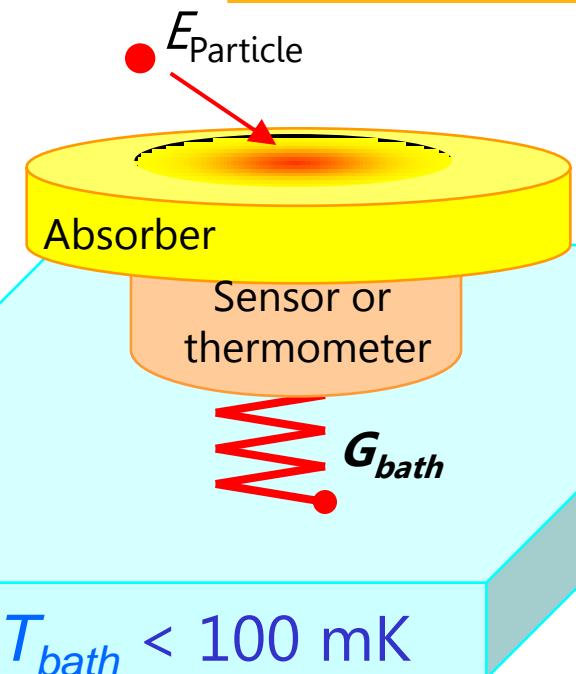
- Beta spectrometry

- MARE project

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# Physical principle of metallic magnetic calorimeters

# Physical principle of calorimeters

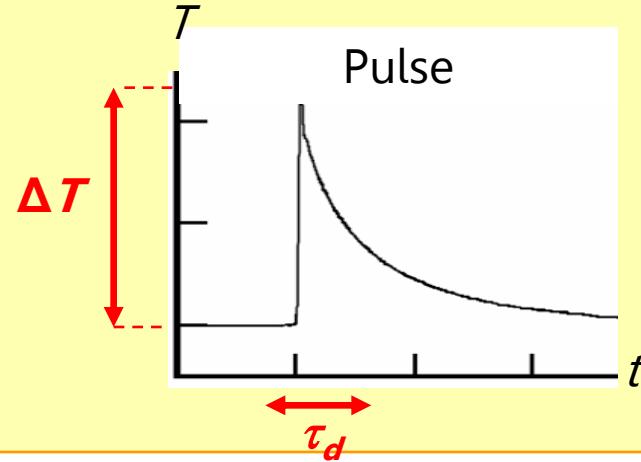


A photon with an energy  $E$  interacts in the absorber

Temperature rise :  $\Delta T = E / C_{\text{total}}$

The detector is weakly thermally coupled to a thermal bath

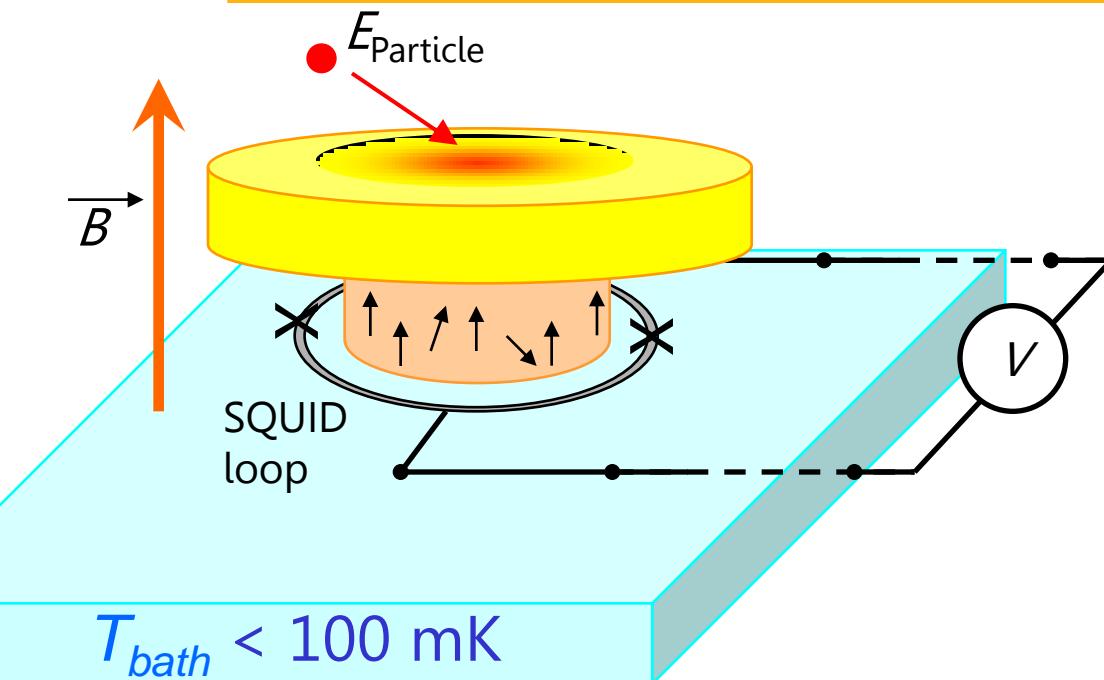
Return to the equilibrium temperature :  $\tau_d = C_{\text{total}} / G_{\text{bath}}$



$$C_{\text{absorber}} = \begin{cases} C_{\text{Electron}} \propto T & \text{(Metal)} \\ C_{\text{Phonon}} \propto T^3 & \text{(Dielectric crystal, superconductor)} \end{cases}$$

→  $\Delta T$  maximised at low  $T_{\text{bath}}$

# Physical principle of magnetic calorimeters



The sensor is a paramagnetic material, magnetized by an external magnetic field  $\mathbf{B}$

The sensor magnetization  $\mathbf{M}$  is strongly dependent on the temperature

Absorption of a particle with the energy  $E$  leads to a temperature rise and a change of  $\mathbf{M}$

A magnetization change induces a flux variation  $\Delta\Phi$  in the SQUID loop

$$\delta\Phi = \frac{G}{r_{\text{loop}}} \cdot \delta m = \frac{G}{r_{\text{loop}}} \cdot \mu_0 \cdot V_{\text{sensor}} \cdot \left( \frac{\partial M}{\partial T} \right) \frac{E_{\text{particle}}}{C_{\text{sensor}} + C_{\text{absorber}}}$$

Magnetic coupling factor

Thermodynamic quantities of paramagnetic material  
 $f(B, T, V_{\text{sensor}}, x)$

## Calculation of thermodynamics quantities using statistical physics

Example for localized spin of 1/2 interacting with  $B$

Zeeman Hamiltonian  $H^{\text{Zeeman}} = -\vec{\mu} \cdot \vec{B}$

Two eigen energies  $\varepsilon_{\pm} = \pm \mu B$        $\Delta E = \varepsilon_+ - \varepsilon_-$

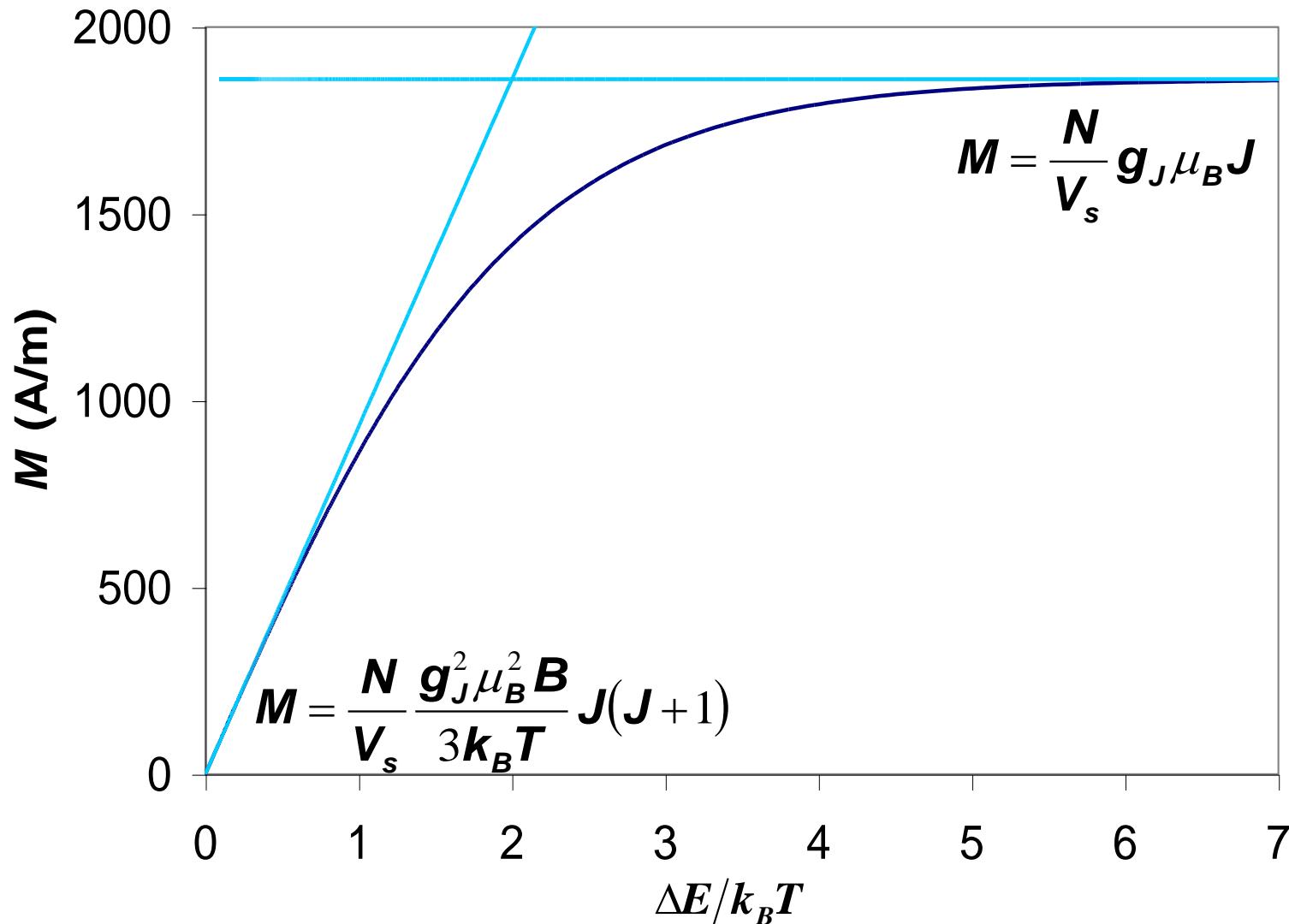
Partition function of a canonical ensemble  $Z = \sum_{n=-J}^J e^{-\varepsilon_n/kT}$

Internal energy  $\langle U \rangle = N \langle \varepsilon \rangle = N k_B T^2 \left( \frac{\partial \ln Z}{\partial T} \right)_B = -N \cdot \Delta E \tanh \left( \frac{\Delta E}{2k_B T} \right)$

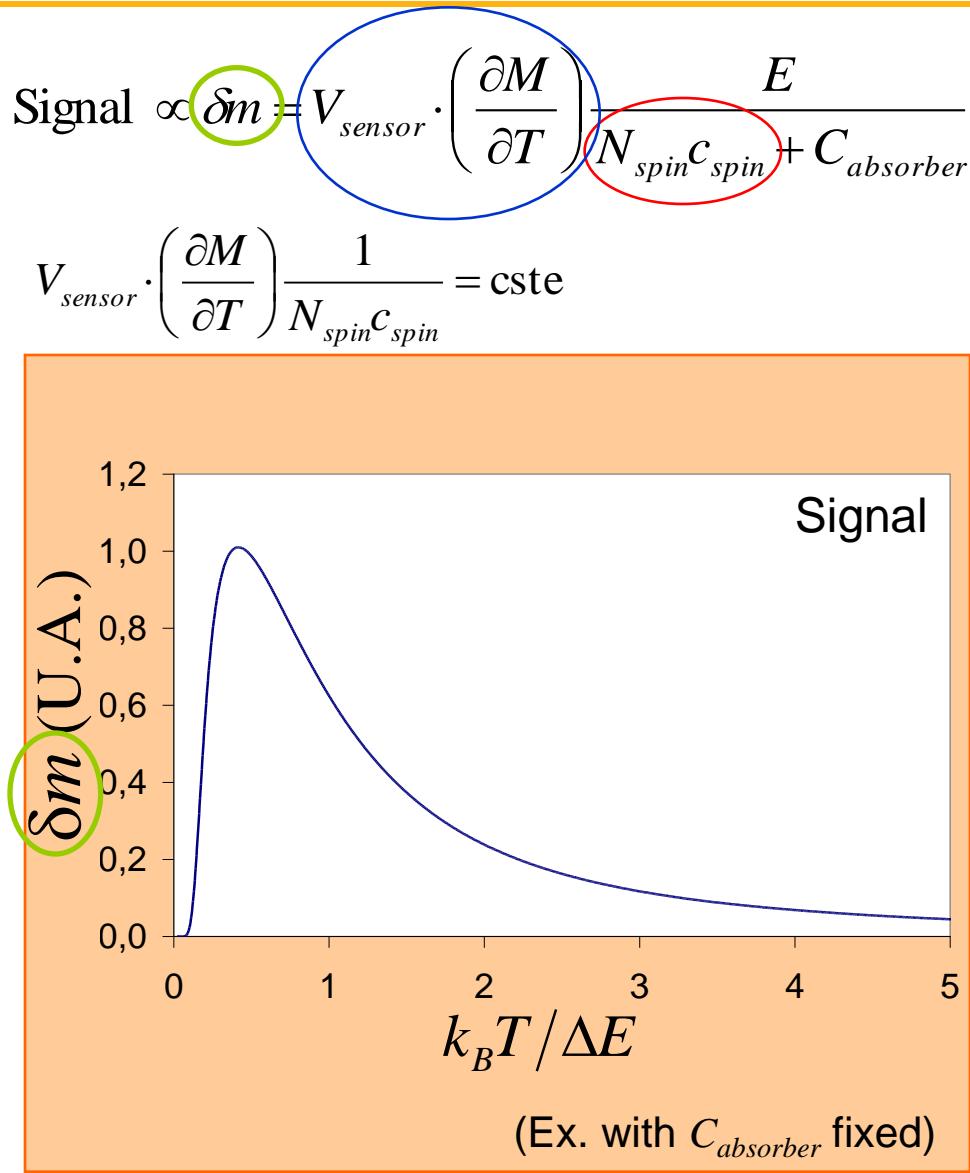
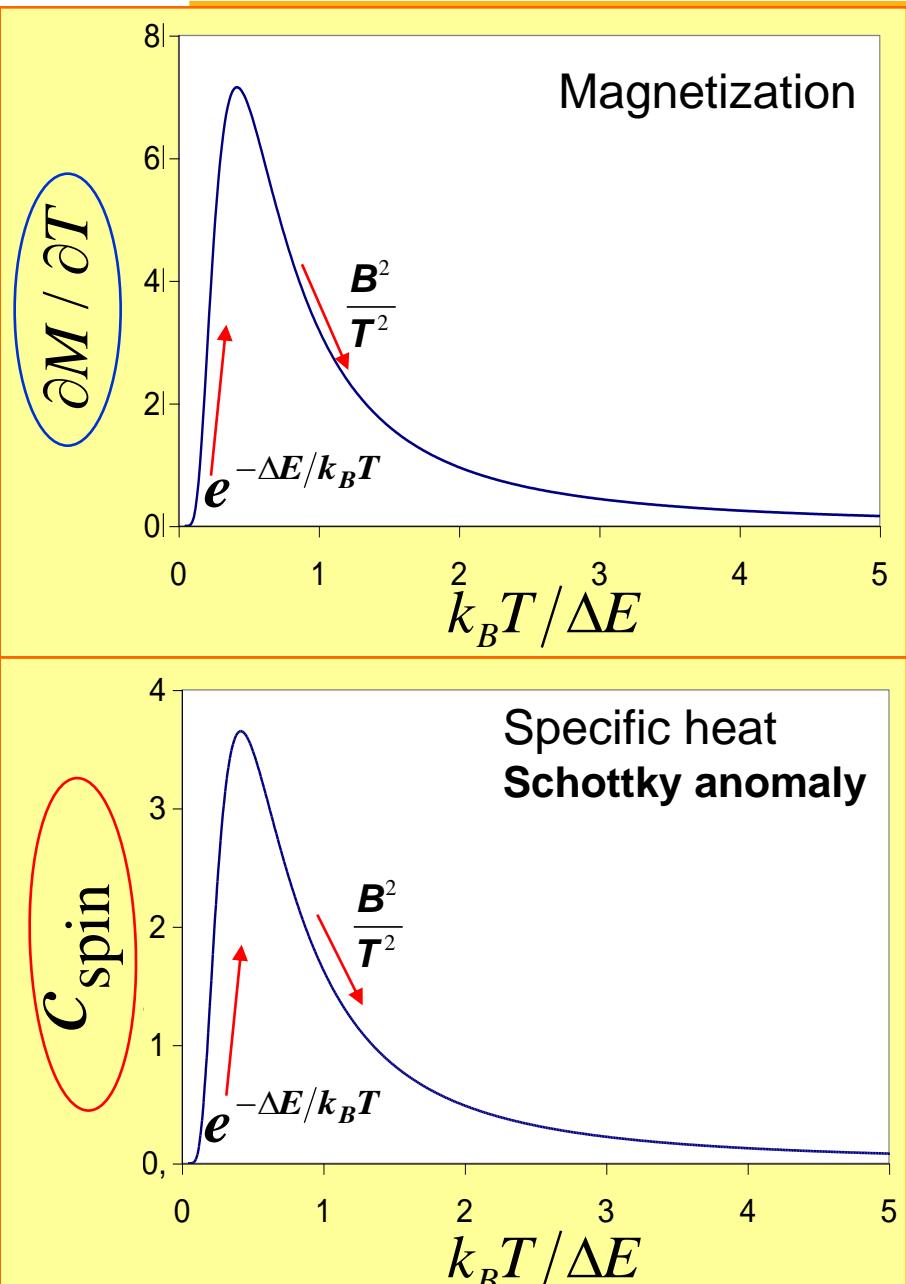
Magnetization  $M = -\frac{N_{\text{spin}}}{V_{\text{sensor}}} \frac{\partial \langle U \rangle}{\partial B} = \frac{N_{\text{spin}}}{V_{\text{sensor}}} \frac{\Delta E}{2B} \tanh \left( \frac{\Delta E}{2k_B T} \right)$

Spin heat capacity  $C_{\text{spin}} = \left( \frac{\partial \langle U \rangle}{\partial T} \right)_V = N_{\text{spin}} k_B \left( \frac{\Delta E}{2k_B T} \right)^2 \frac{1}{\cosh^2(e^{\Delta E/2k_B T})} \approx C_{\text{sensor}}$

# Magnetization



# Thermodynamics quantities for the signal



→ Possibility to use large  $C_{spin}$  and couple absorber with large  $C_{absorber}$

# Ideal magnetic calorimeters for spectrometry

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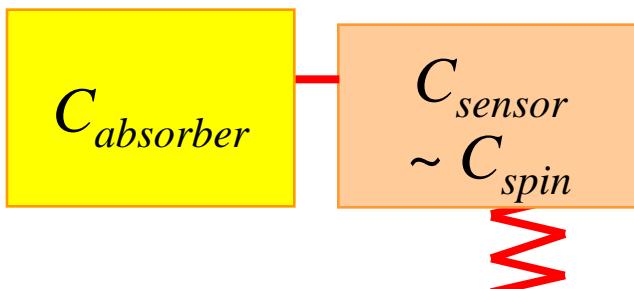
Each application requires a detection efficiency which fixes the absorber heat capacity.

One has to calculate the parameters  $B$ ,  $T_{bath}$ ,  $x$ ,  $V_{sensor}$ , that maximize the Signal/Noise ratio.

For spectrometry applications one needs a fast rise time and high energy resolution.

## Ideal magnetic calorimeters :

- Large signal  $\leftrightarrow$  strong dependence of the magnetization on the temperature  
 $\leftrightarrow$  No interaction between magnetic moments  
No additional heat capacities  $C_{sensor} = C_{spin}$
- Fast rise time  
 $\leftrightarrow$  Strong coupling between spins and the absorber heat capacity  
large  $G_{sensor-absorber}$



# Different choices of magnetic ions and host

11

- Dielectric host
  - TmAG:Er, YAG:Er
  - CMN, CDP

**High sensitivity but very long rise time** due to a weak coupling between magnetic moments and phonons
- Metallic host
  - LaB<sub>6</sub>:Er (large additional heat capacity at low  $T$ )
  - **Au:Er (well known, stable)**
  - Ag:Er

**Reduced sensitivity** due to exchange interaction between magnetic moments  
**but fast rise time** due to strong coupling between magnetic moments and conduction electrons
- Semi metallic host (unstudied)
- Semiconductor (unstudied)
  - Bi<sub>2</sub>Te<sub>3</sub> ( $E_g = 0,15$  eV) doped with Er

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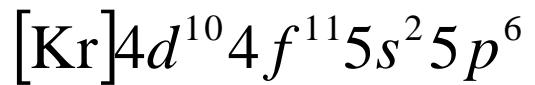
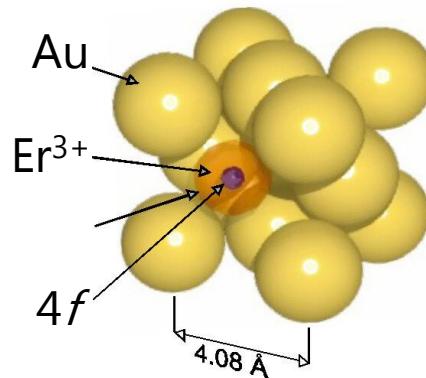
# Signal size for Metallic Magnetic Calorimeter using Au:Er sensor

# Magnetic properties of AuEr. Er in cubic symmetry

- Electronic Zeeman interaction

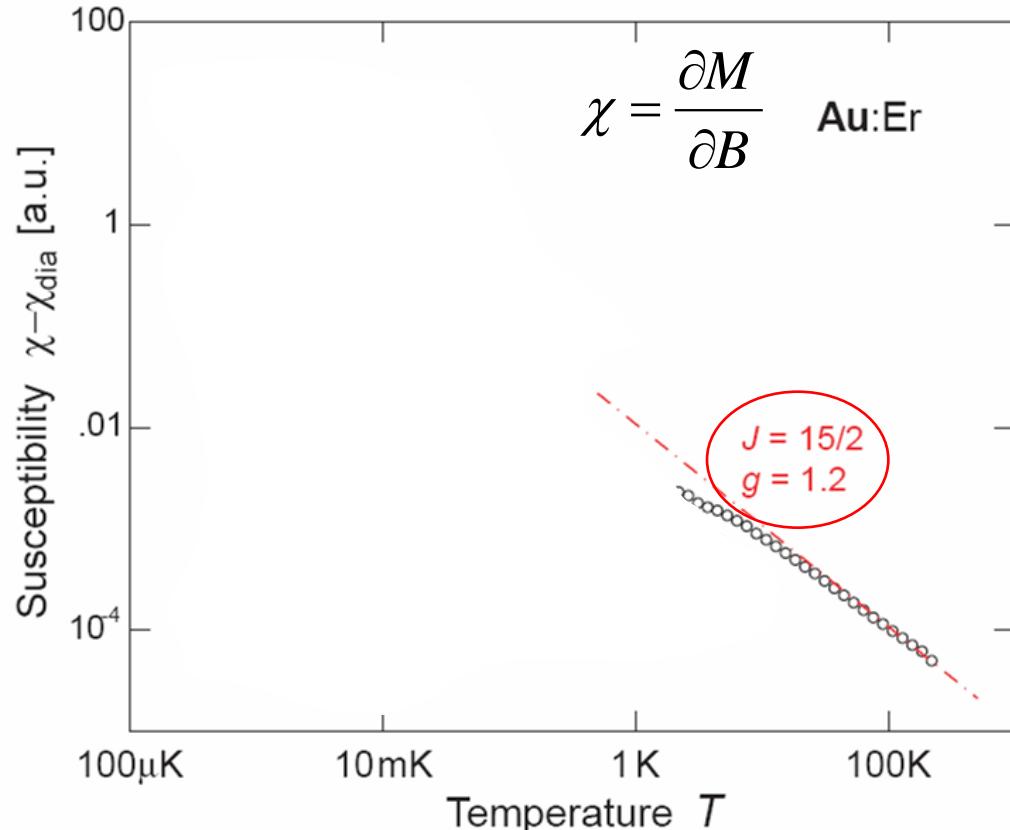
$$J = 15/2 \quad g_J = 6/5$$

$$H^{Zeeman} = g_J \mu_B \vec{B} \cdot \vec{J}$$



$$\langle r_{4f} \rangle \approx 0.3 \text{ \AA}^\circ$$

$$\langle r_{5p} \rangle \approx 1 \text{ \AA}^\circ$$



# Exchange interactions

Interaction between two localized spins  $S_i$  and  $S_j$

- Dipole – Dipole interaction

Coupling between two localized magnet

$$H_{ij}^{Dipole} = \underbrace{\frac{\mu_0}{4\pi} (\tilde{g}\mu_B)^2 (2k_F)^3}_{\Gamma_{\text{Dipole}}} \frac{\left( \vec{\tilde{S}}_i \cdot \vec{\tilde{S}}_j \right) - 3 \left( \vec{\tilde{S}}_i \cdot \vec{r}_{ij} \right) \left( \vec{\tilde{S}}_j \cdot \vec{r}_{ij} \right)}{(2k_F r_{ij})^3}$$

- RKKY interaction (Ruderman - Kittel - Kasuya - Yosida)

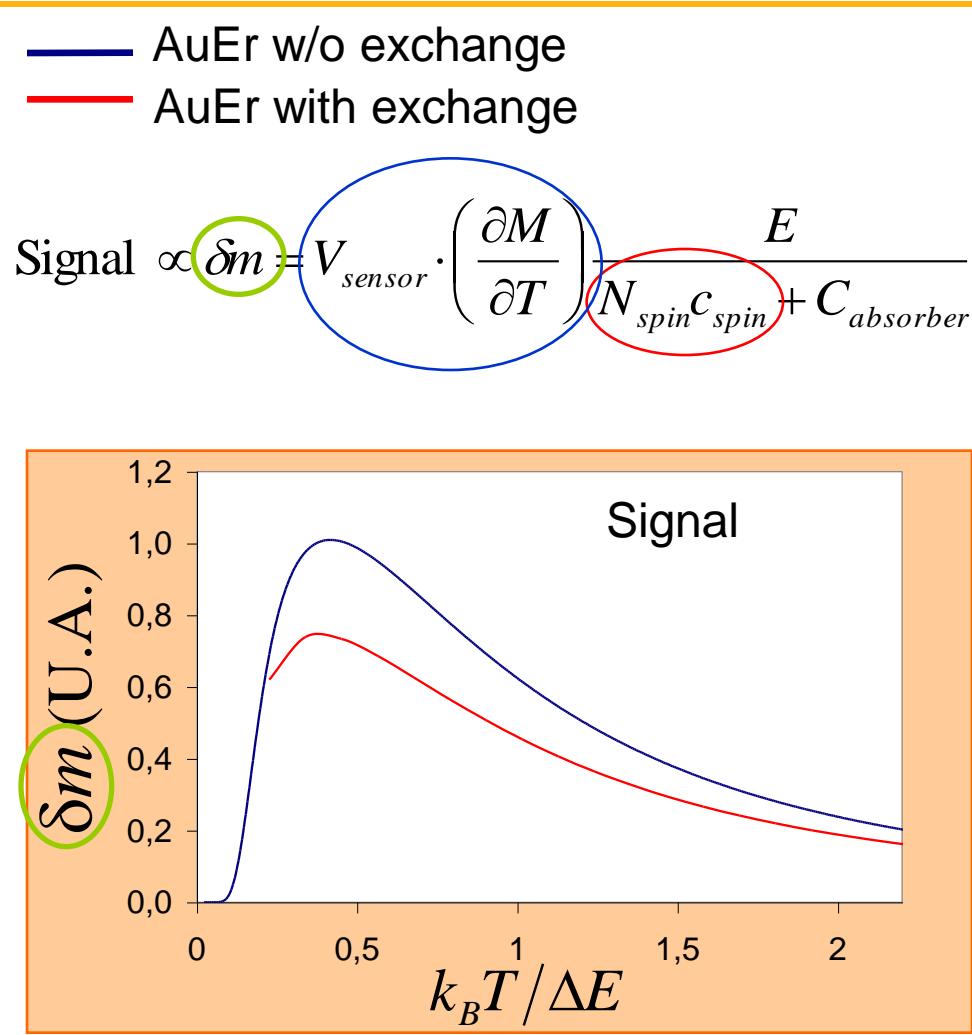
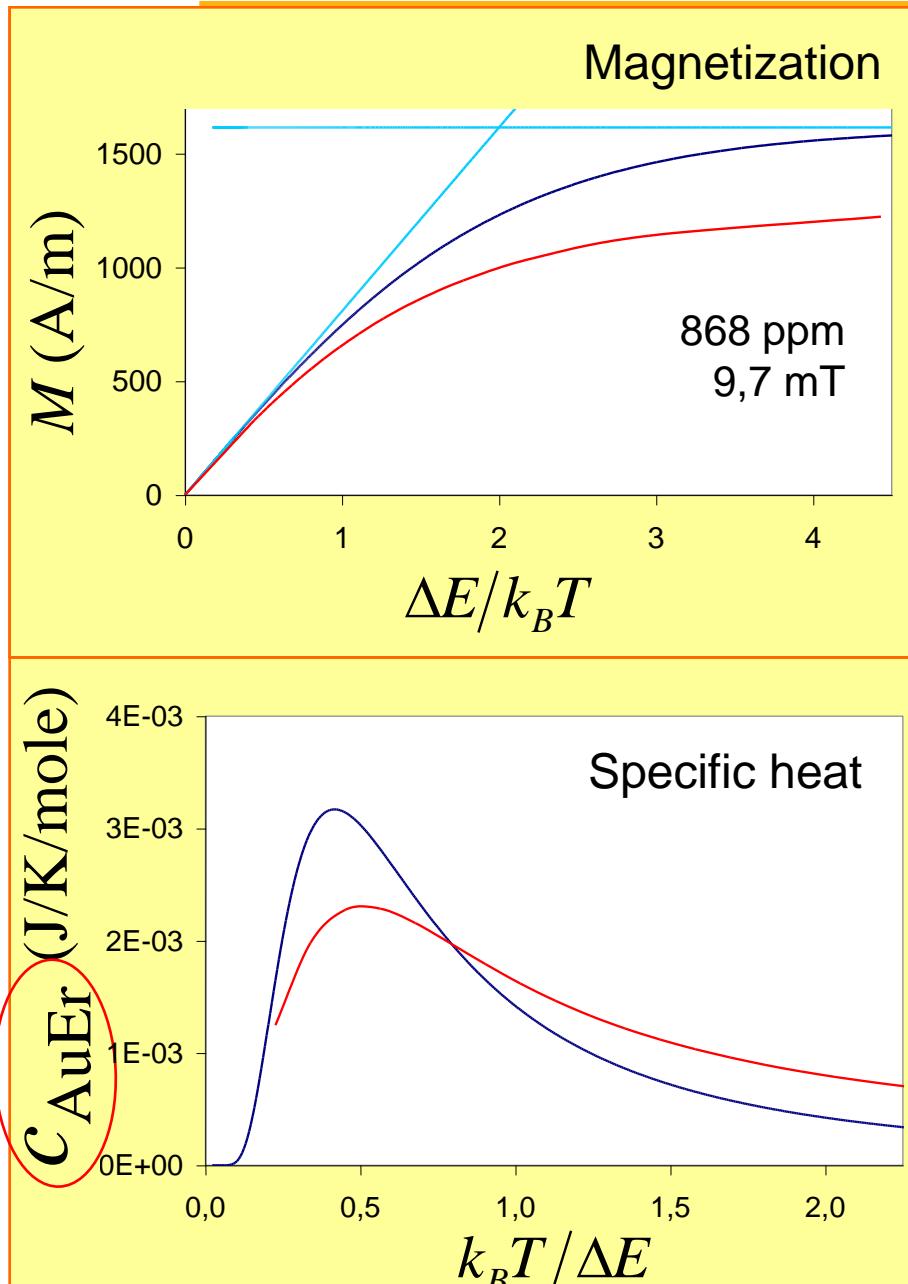
Interaction between two localized magnetic moments mediates through the conduction electrons and their magnetic moment (itinerant electrons).

$$H_{ij}^{RKKY} = \underbrace{J_{sf}^2 \frac{\tilde{g}^2 (g_J - 1)^2}{g_J^2} \frac{4V_p^2 m_e^* k_F^4}{\hbar^2 (2\pi)^3}}_{\Gamma_{\text{RKKY}}} \left( \vec{\tilde{S}}_i \cdot \vec{\tilde{S}}_j \right) \frac{\cos(2k_F r_{ij}) - 1/2 k_F r_{ij} \cdot \sin(2k_F r_{ij})}{(2k_F r_{ij})^3}$$

$$\Gamma_{\text{RKKY}} = 5 \cdot \Gamma_{\text{Dipole}}$$

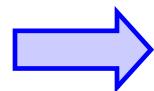
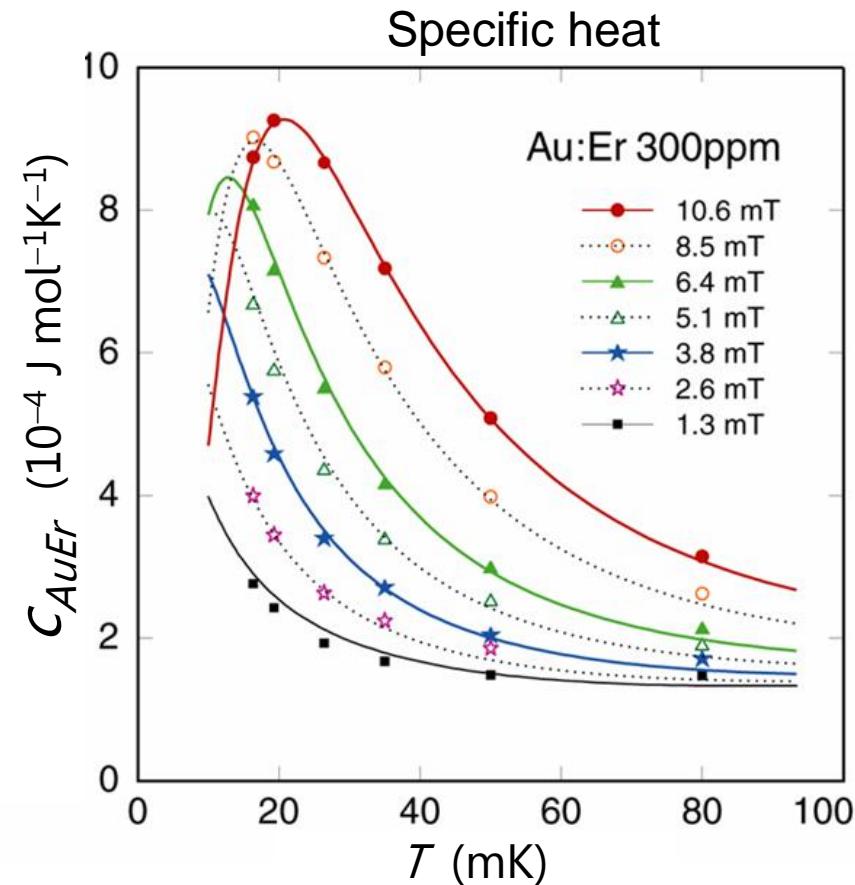
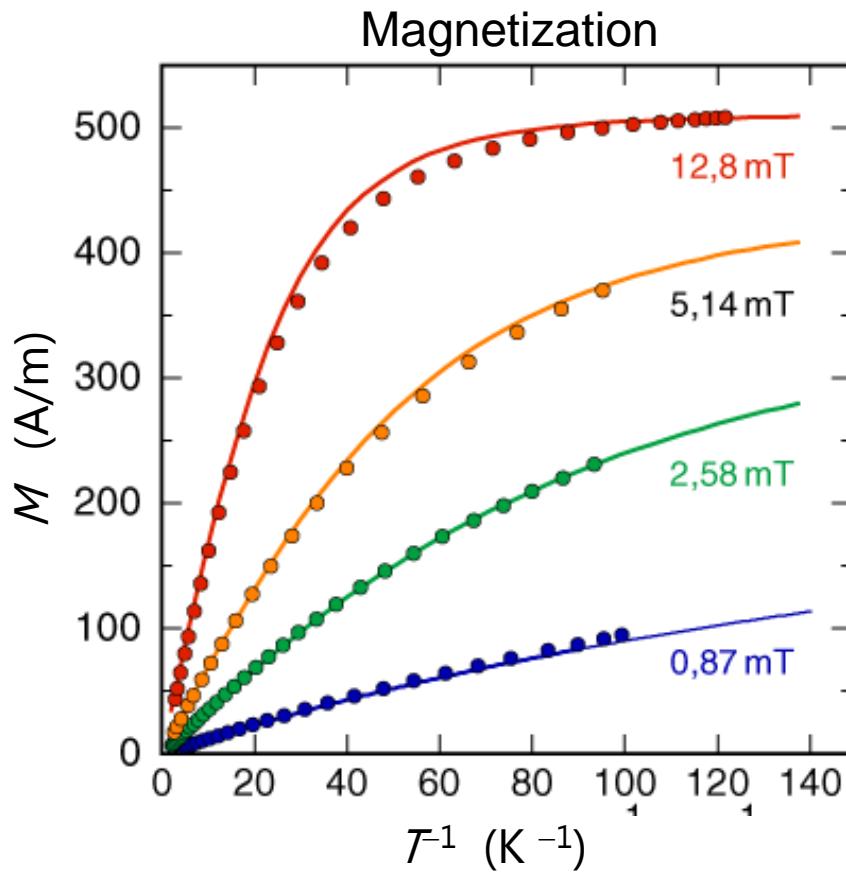
RKKY interaction leads to spin glass transition at  $\sim 1$  mK with 300 ppm erbium  
 minimal  $T_{\text{bath}} \sim 10$  mK

# Thermodynamic quantities for the signal



→ Exchange interactions lead to a reduced of the signal size

Thermodynamic properties of AuEr can be calculated by mean field approximations or with Monte Carlo simulations.

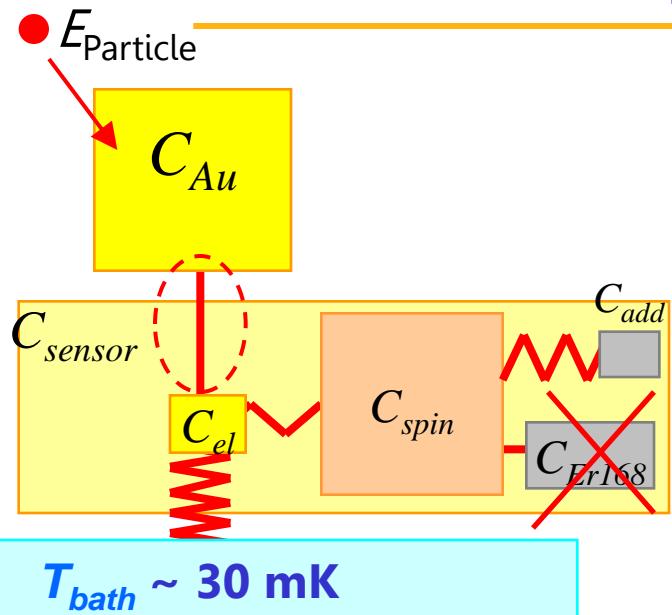


We can predict the signal size  
as a function of all the parameters

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# Time structure of the signal

# Heat capacities and thermal conductances



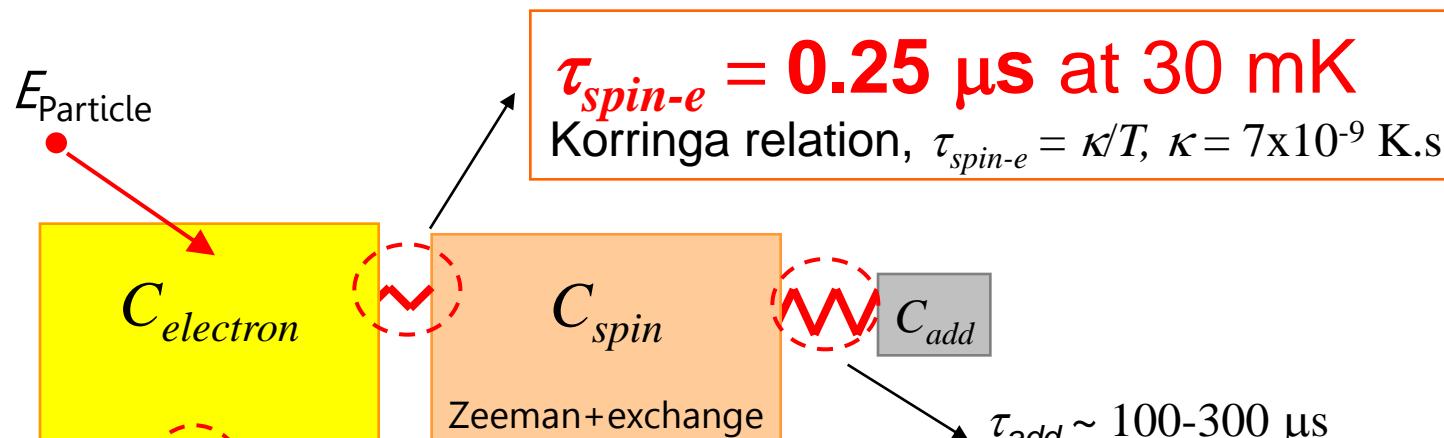
If we use a gold absorber

- $C_{\text{Au}} = N \left( \gamma T + 234 \cdot k_B N_a \left( \frac{T}{\theta_D} \right)^3 \right)$   $\gamma = 7.29 \cdot 10^{-4} \text{ J/K}^2/\text{mole}$   $\theta_D = 162.4 \text{ K}$
- $C_{\text{spin}}$  electronic magnetic moments (Zeeman+exchange)
- $C_{\text{el}}$  conduction electrons of Au:Er ( $\sim 1\%$  of  $C_{\text{spin}}$ )
- $C_{\text{add}}$  : interaction of the nuclear quadrupole moments of gold with the electric field gradient due to the presence of  $\text{Er}^{3+}$
- $C_{\text{Er}168}$  : hyperfine interactions of the nuclear magnetic moments of  $\text{Er}^{168}$ . Using of enriched  $\text{Er}^{166}$  or  $\text{Er}^{167}$

$x = 900 \text{ ppm}$ $B \sim 5 \text{ mT}$	$c_{\text{Au}}$ mJ/K/mole	$c_{\text{spin}}$ mJ/K/mole	$c_{\text{add}}$ mJ/K/mole
20 mK	0.015	1.8	$\sim 1/4 c_{\text{spin}}$
30 mK	0.022	1.4	$\sim 1/5 c_{\text{spin}}$

# Thermalisation of the particle energy and pulse shape

We suppose heat diffusion through conduction electrons very fast



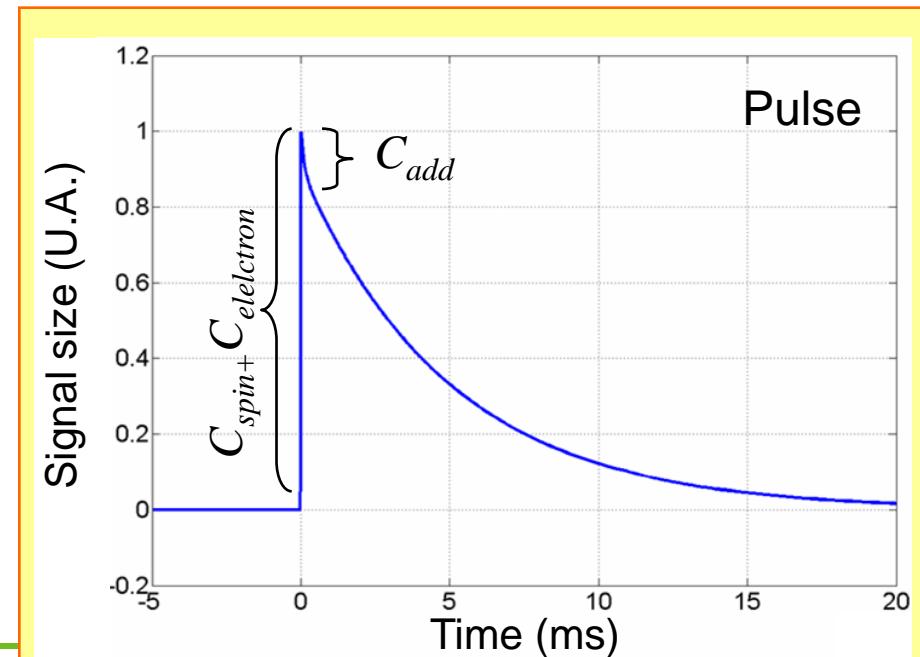
$$\tau_{\text{spin-e}} = 0.25 \mu\text{s} \text{ at } 30 \text{ mK}$$

Korringa relation,  $\tau_{\text{spin-e}} = \kappa/T$ ,  $\kappa = 7 \times 10^{-9} \text{ K.s}$

$T_0 \sim 30 \text{ mK}$

$$\tau_d = C_{\text{total}} / G$$

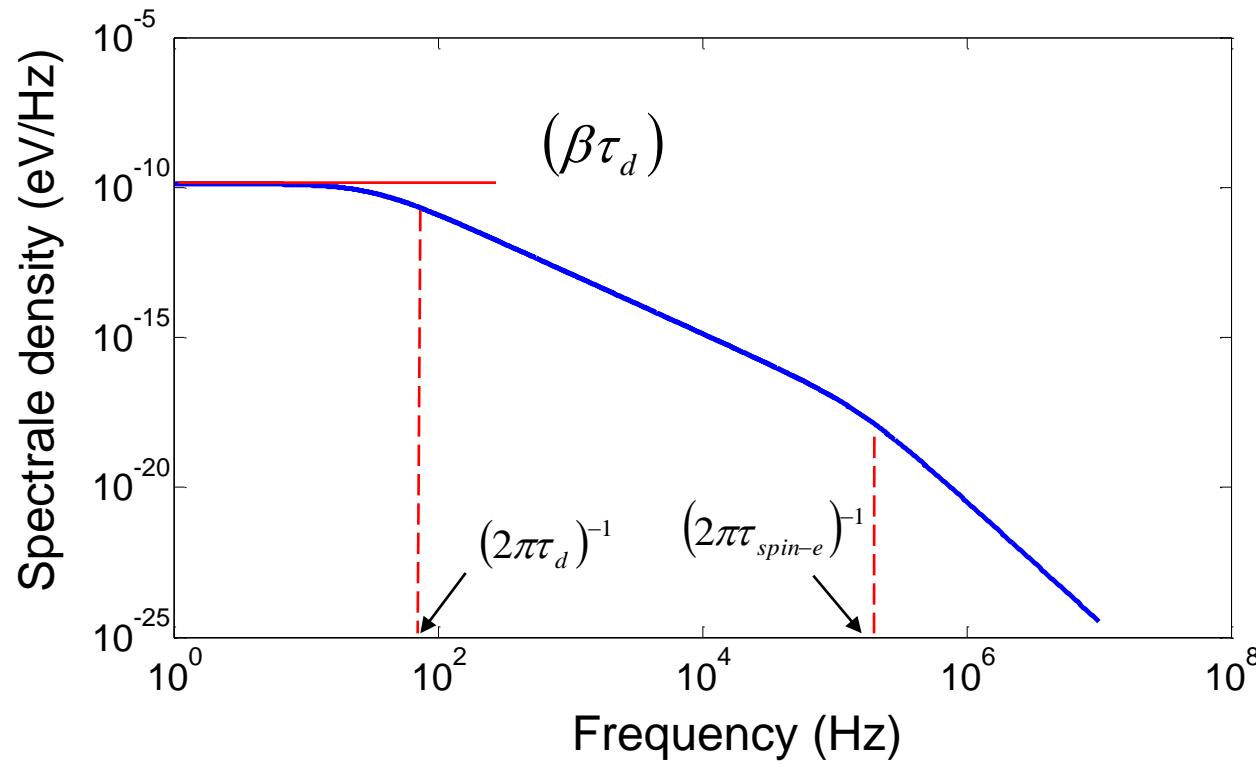
$G_{\text{Kapitza}} \sim 10 \text{ nW/K/mm}^2$  at 20 mK  
 $G_{\text{metal-metal}} \text{ preferable, } \gg G_{\text{Kapitza}}$



# Fourier spectrum of the signal

$$S(f) = E \frac{(\beta \tau_d)}{\sqrt{(1 + (2\pi f \tau_r)^2)(1 + (2\pi f \tau_r)^2)}}$$

$$\beta = \frac{C_{spin}}{C_{spin} + C_{electron}}$$



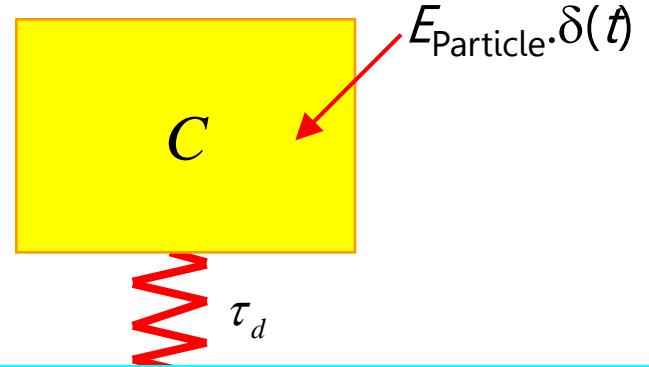
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# Intrinsic sources of noise

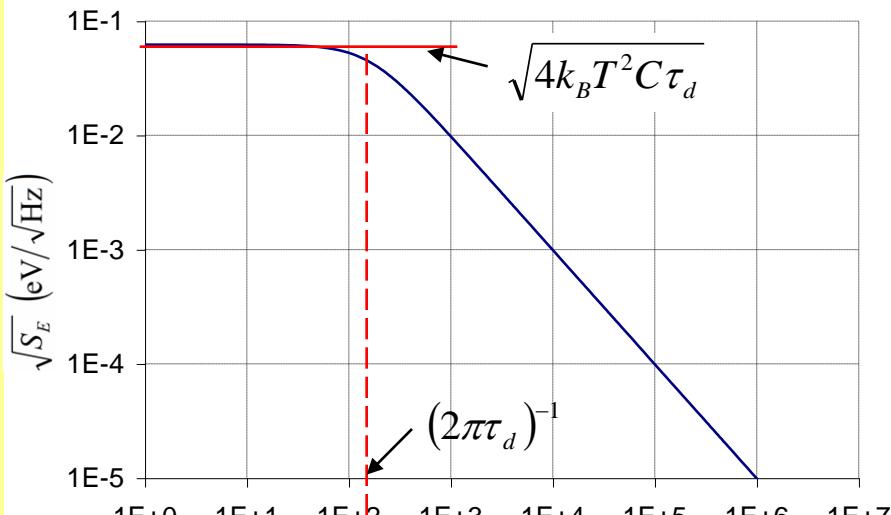
# Thermodynamic fluctuations of the energy

A simple canonical ensemble with one system.

$$\Delta U = \sqrt{\langle U^2 \rangle - \langle U \rangle^2} = \sqrt{k_B T^2 \left( \frac{\partial \langle U \rangle}{\partial T} \right)} = \sqrt{k_B T^2 C}$$



→ Low Temperature required!



$$T = 30 \text{ mK}, C = 1 \text{ pJ/K}, \tau_d = 1 \text{ ms}$$

$$S_E = k_B C T^2 \frac{4\tau_d}{(1 + 2\pi f \tau_d)^2}$$

# Thermodynamic fluctuations of the energy

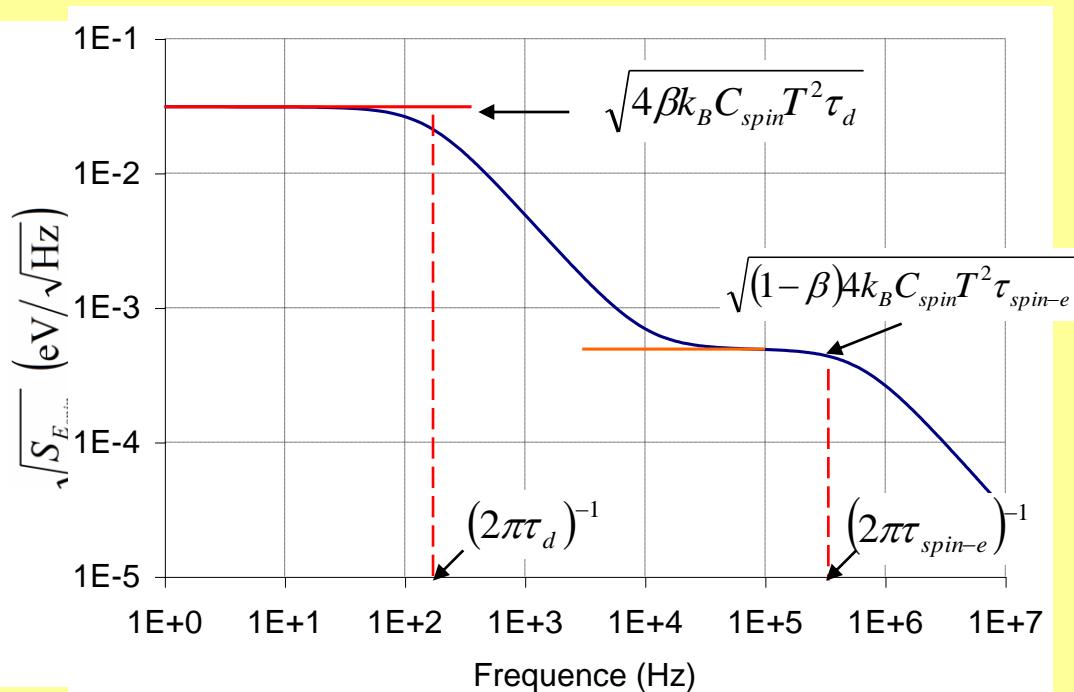
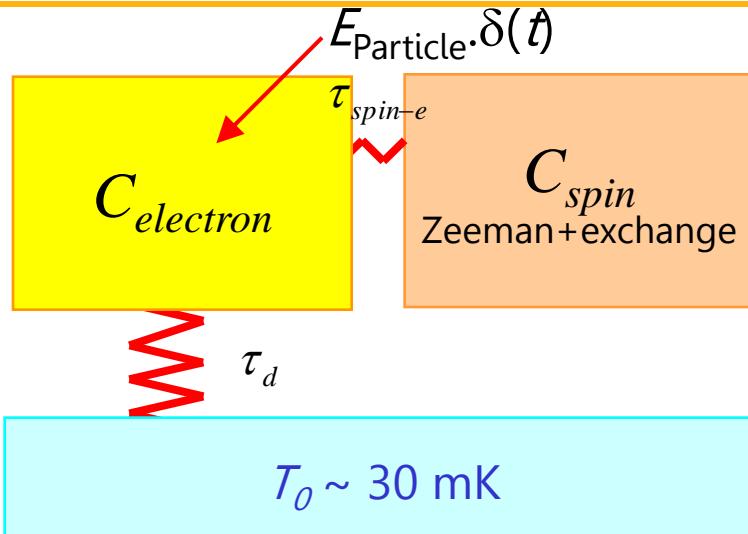
Canonical ensemble with two sub systems

( $C_{add}$  ignored).

$$\beta = \frac{C_{spin}}{C_{spin} + C_{electron}}, 0.1 < C_{spin}/C_{electron} < 10, \tau_{spin-e} \ll \tau_d$$

$$S_{spin} = k_B C_{spin} T^2 \left[ (1-\beta) \frac{4\tau_{spin-e}}{1 + (2\pi f \tau_{spin-e})^2} + \beta \frac{4\tau_d}{(1 + 2\pi f \tau_d)^2} \right]$$

**Low Temperature required!**



$$C_{electron} = C_{spin} = 0.5 \text{ pJ/K}, T = 30 \text{ mK},$$

$$\tau_{spin-e} = 0.25 \mu\text{s}, \tau_d = 1 \text{ ms}$$

Fundamental limits of metallic magnetic calorimeter :

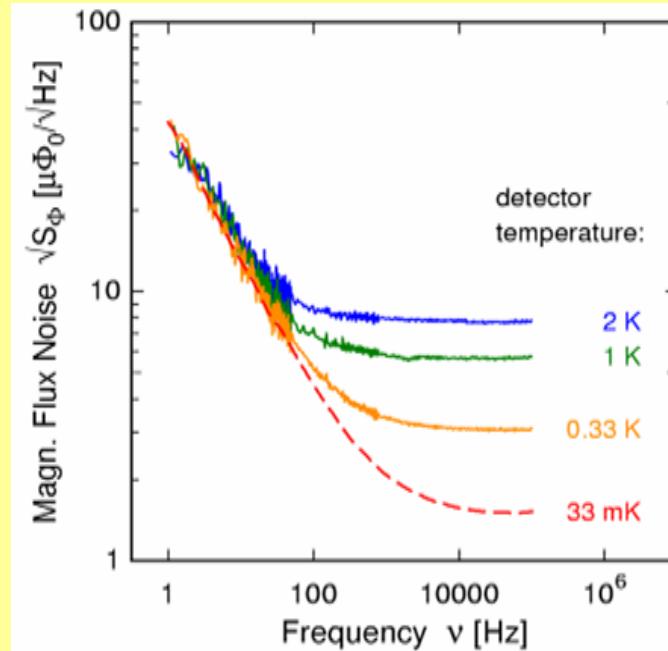
$$\Delta U_{spin} = \sqrt{4k_B T^2 C_e} \left( \frac{1}{\beta(1-\beta)} \left( \frac{\tau_{spin-e}}{\tau_d} \right)^{1/4} \right)$$

Minimized for  $C_{electron} = C_{spin}$

## Other intrinsic sources of noise

1/f noise of Au:Er sensor

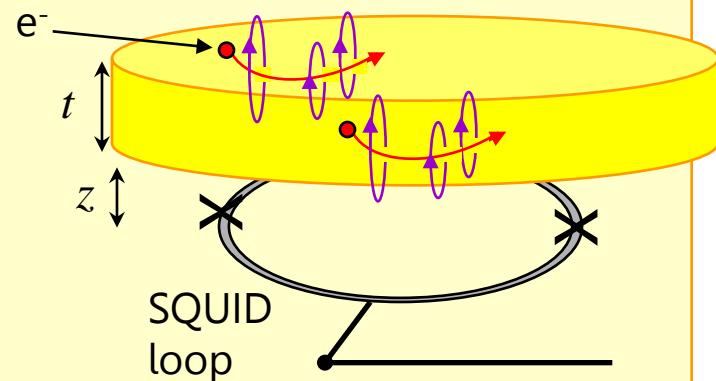
Independent of temperature and proportional to erbium concentration

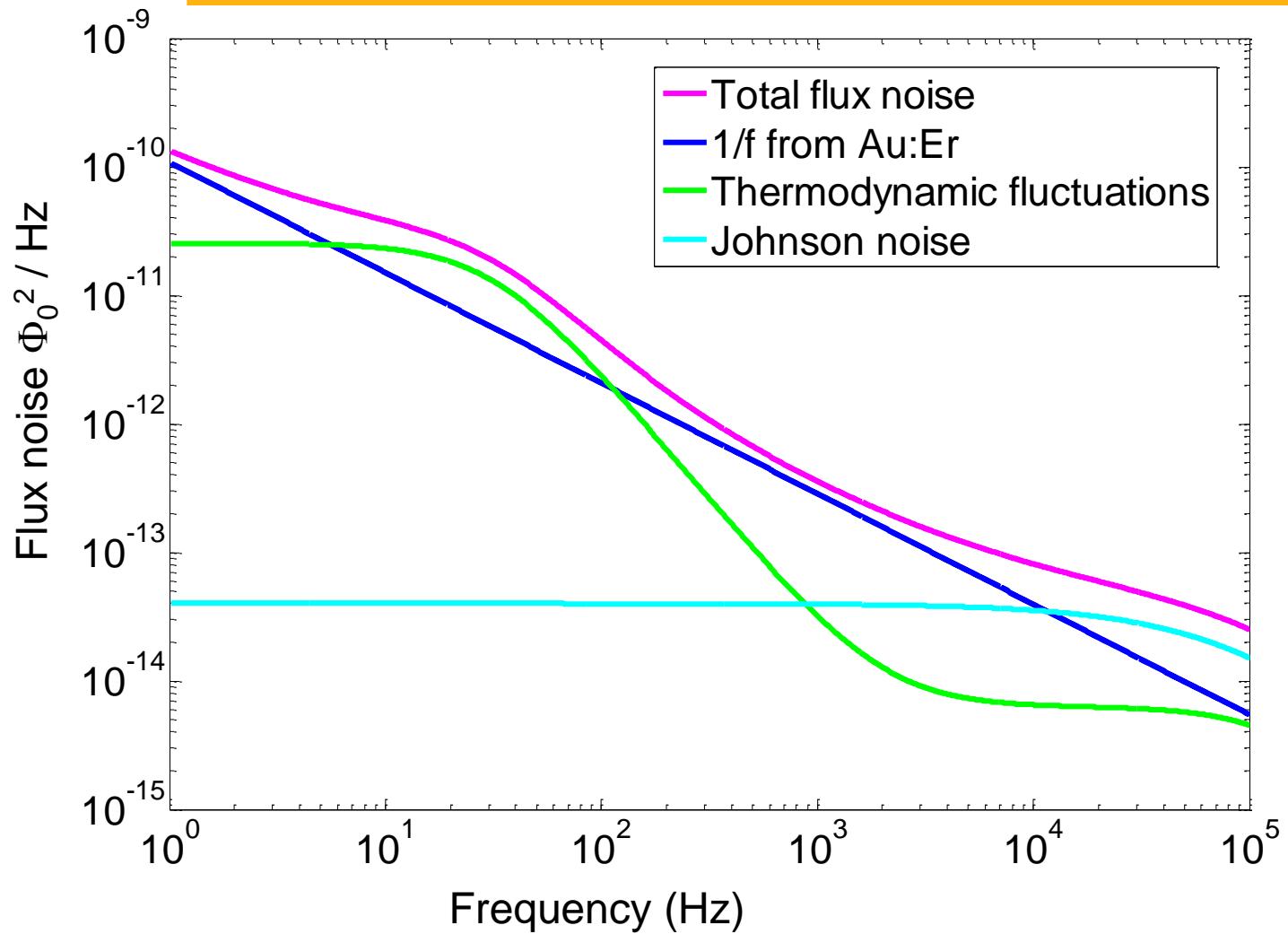


Magnetic Johnson noise, random motion of conduction electrons in metals from the sensor and the absorber

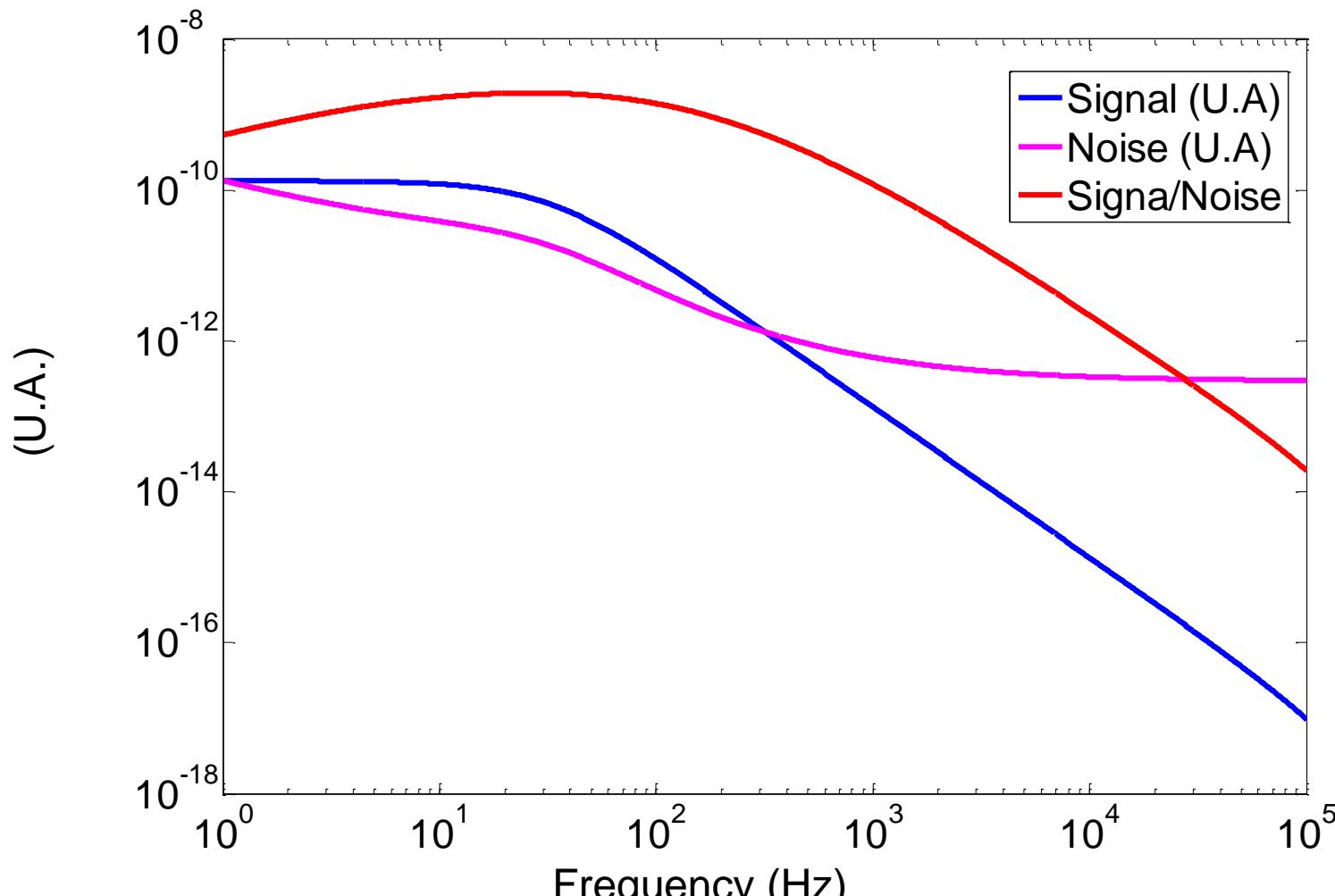
$$\sqrt{S_{\Phi}^{mag}} \approx \mu_0 \sqrt{\alpha \sigma k_B T V} \quad f_c \approx \frac{1}{4 \cdot \mu_0 \cdot \sigma \cdot z \cdot t}$$

Depends strongly on the way the sensor is coupled to the SQUID





# Signal to noise ratio



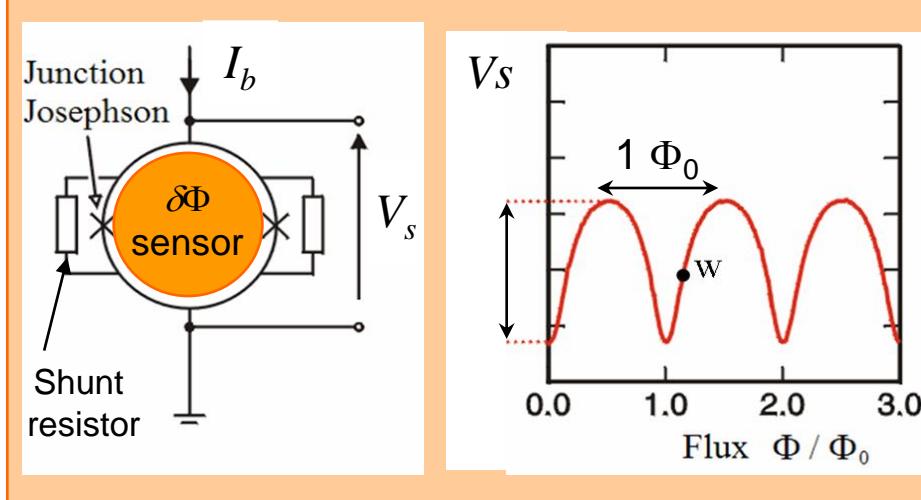
➡ **FWHM = 35 eV**

(Fundamental limit from thermodynamic fluctuations FWHM = 24 eV)

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# How to read the magnetization of the sensor

# SQUID

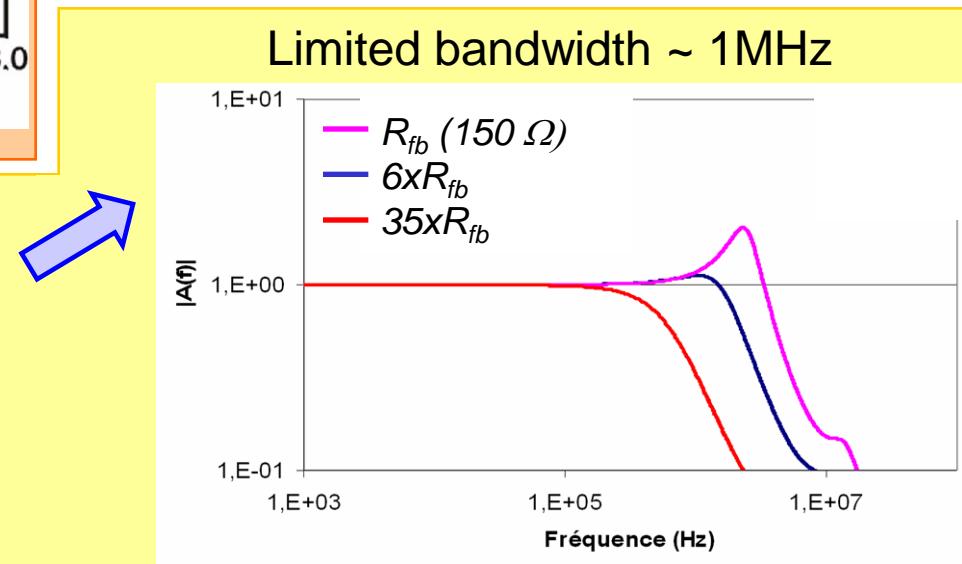
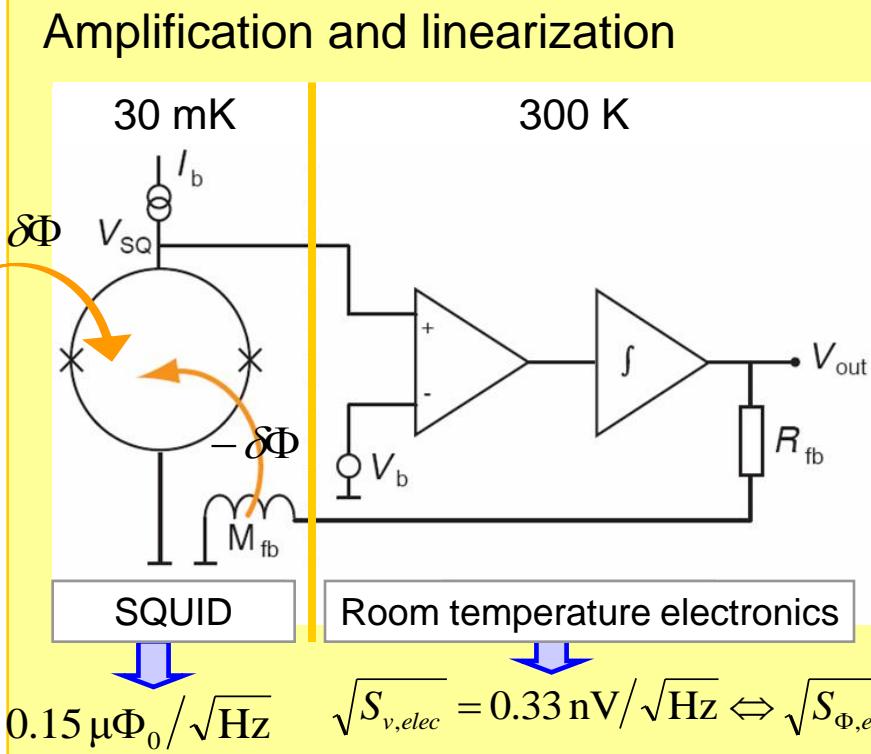


## SQUID Noise

$$S_{\Phi,SQUID} \approx 32 \cdot k_B T \sqrt{L_{SQUID}^3 C_{SQUID}}$$

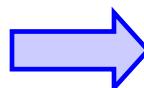
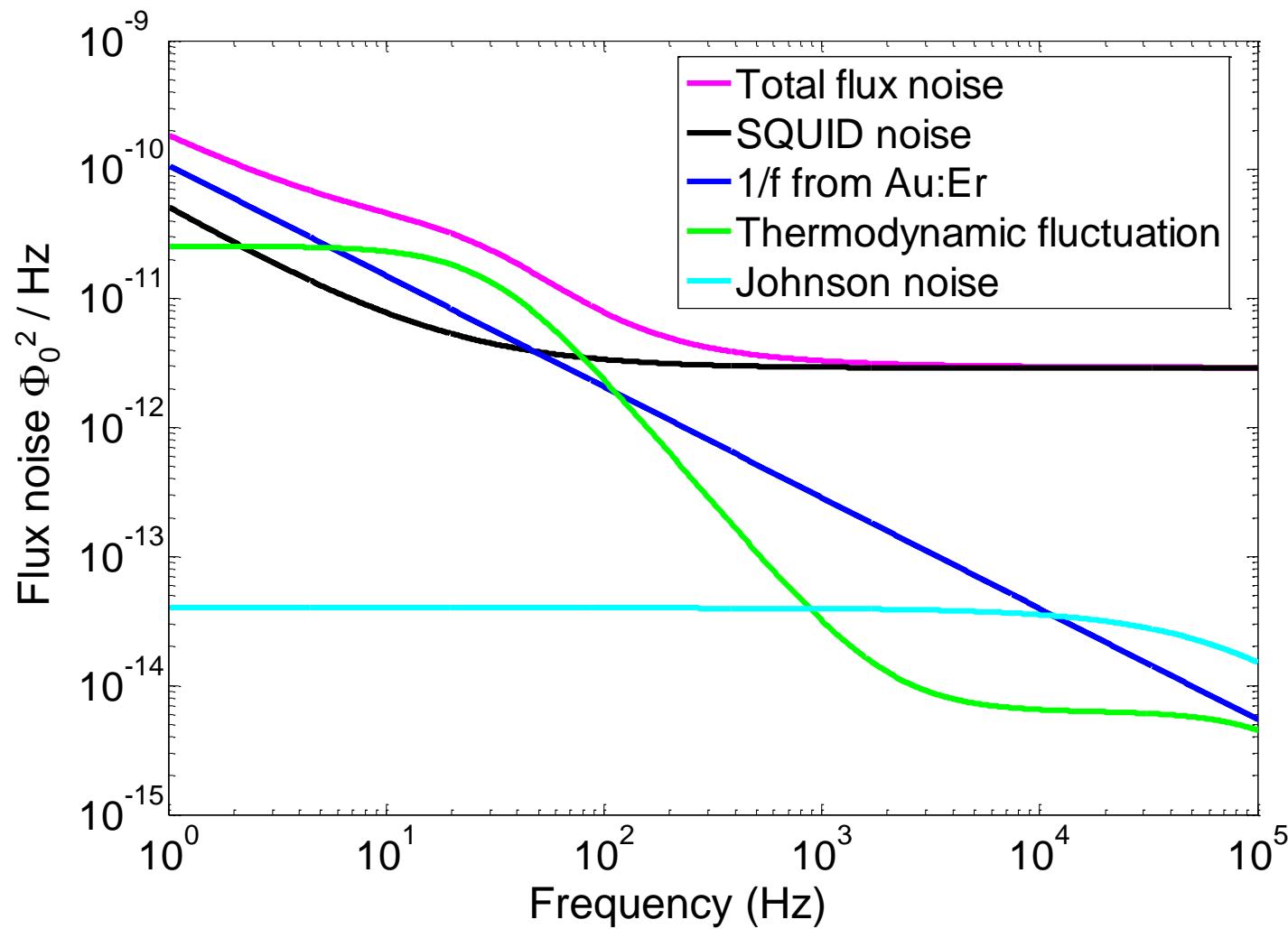
$$L_{squid} \approx 100 \text{ pH}, C_{squid} \approx 1 \text{ pF}, T_{min} \approx 100 \dots 300 \text{ mK}$$

$$\Rightarrow \sqrt{S_{\Phi,SQUID}} \approx 0.15 \mu\Phi_0 / \sqrt{\text{Hz}}$$



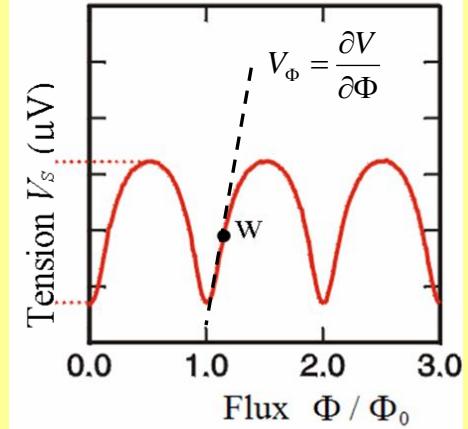
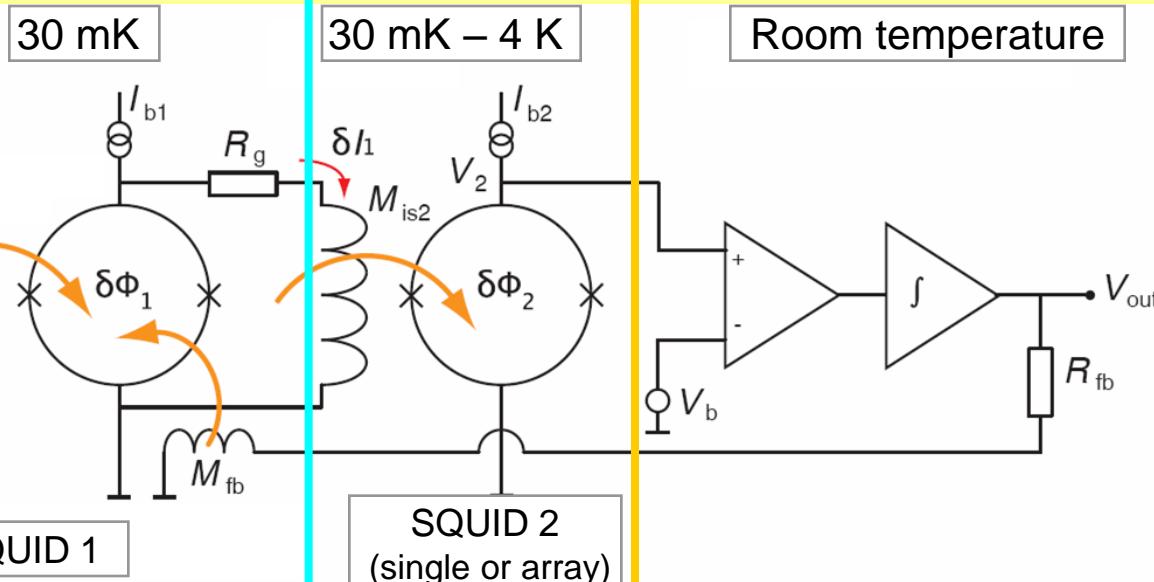
**Slew rate <  $1\Phi_0/\mu\text{s}$ , rise time ~ 1 μs  
Maximal signal size ~  $1\Phi_0$**

$\sqrt{S_{v,elec}} = 0.33 \text{ nV}/\sqrt{\text{Hz}} \Leftrightarrow \sqrt{S_{\Phi,elec}} = 1.7 \mu\Phi_0 / \sqrt{\text{Hz}}$  → **Noise limited by room temperature electronics**



**FWHM = 69 eV**, SQUID electronics white noise of  $1.7 \mu\Phi_0 / \text{Hz}^{1/2}$   
(FWHM = 35 eV with a noiseless electronics)

## Two stage SQUID set up



$$V_\Phi = \frac{\partial V}{\partial \Phi}$$

$$G_\Phi = \frac{\partial \Phi_2}{\partial \Phi_1} \approx \frac{M_{is2}}{R_g + R_S} V_{\Phi,1}$$

$$S_{\Phi,SQUID} = \underbrace{S_{\Phi,1}}_{(0.15 \times 10^{-6})^2} + \underbrace{\frac{4k_B T R_g}{V_{\Phi,1}^2}}_{<(2 \cdot 10^{-8})^2} + \underbrace{\frac{S_{\Phi,2}}{G_\Phi^2}}_{(0.08 \dots 0.7 \times 10^{-6})^2} + \underbrace{\frac{S_{V,elec}}{V_{\Phi,2}^2 G_\Phi^2}}_{(0.6 \times 10^{-6})^2}$$

$$\sqrt{S_{\Phi,1}} \approx 0.15 \mu\Phi_0 / \sqrt{\text{Hz}}$$

$$\sqrt{S_{\Phi,2}} \approx 0.15 \dots 2 \mu\Phi_0 / \sqrt{\text{Hz}}$$

$$R_g \approx 1 \dots 50 \Omega$$

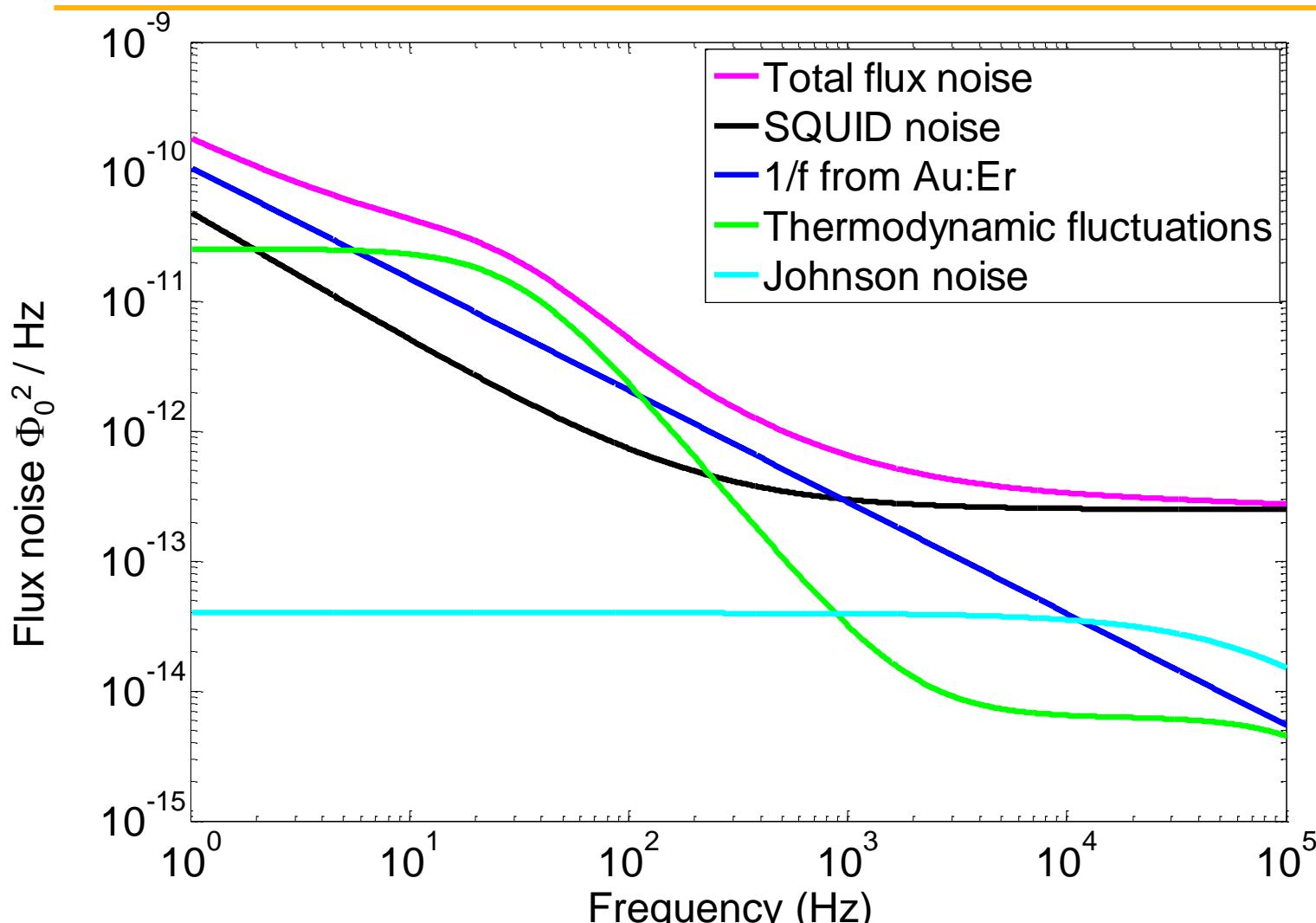
$$\sqrt{S_{V,elec}} \approx 0.33 \mu\text{V} / \sqrt{\text{Hz}}$$

$$V_{\Phi,2} \approx 200 \mu\text{V}/\Phi_0, G_{\Phi,\max} \approx 3$$

$$\sqrt{S_{\Phi,SQUID}} = 0.5 \text{ to } 1 \mu\Phi_0 / \sqrt{\text{Hz}}$$

$$\sqrt{S_{\Phi,SQUID_{1/f}}} (1 \text{ Hz}) \approx 8 \mu\Phi_0 / \sqrt{\text{Hz}}$$

Lower power dissipation in the SQUID1 shunts



→ **FWHM = 45 eV**, SQUID electronics white noise of  $0.5 \mu\Phi_0 / \text{Hz}^{1/2}$   
(FWHM = 35 eV with a noiseless electronics)

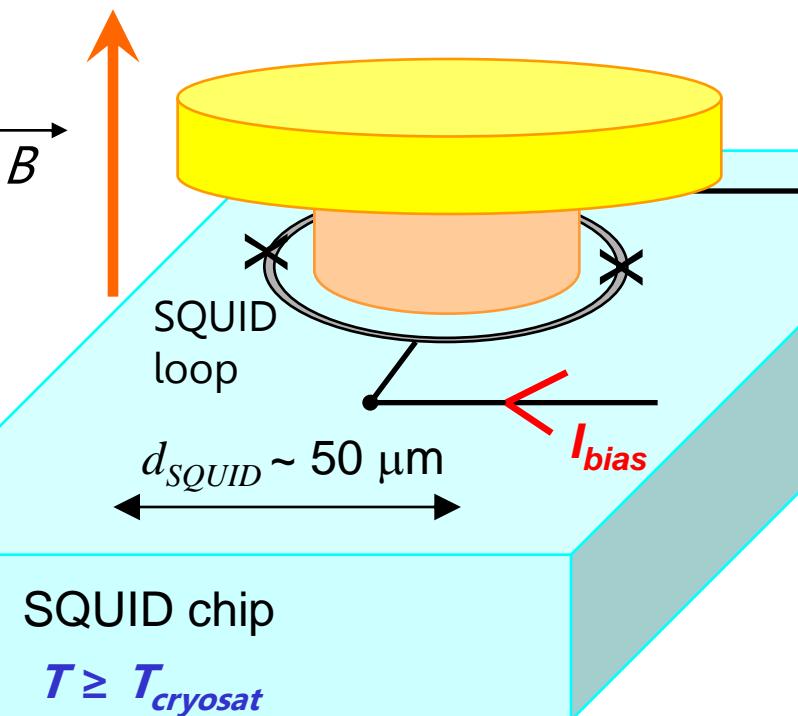
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# **How to couple the magnetization of the sensor to the SQUID**

# Direct coupling

$$\delta\Phi = \frac{G}{r_{loop}} \cdot V_{sensor} \cdot \mu_0 \cdot \left( \frac{\partial M}{\partial T} \right) \frac{E}{C_{sensor} + C_{absorber}}$$

Magnetic coupling factor between the sensor and the SQUID loop



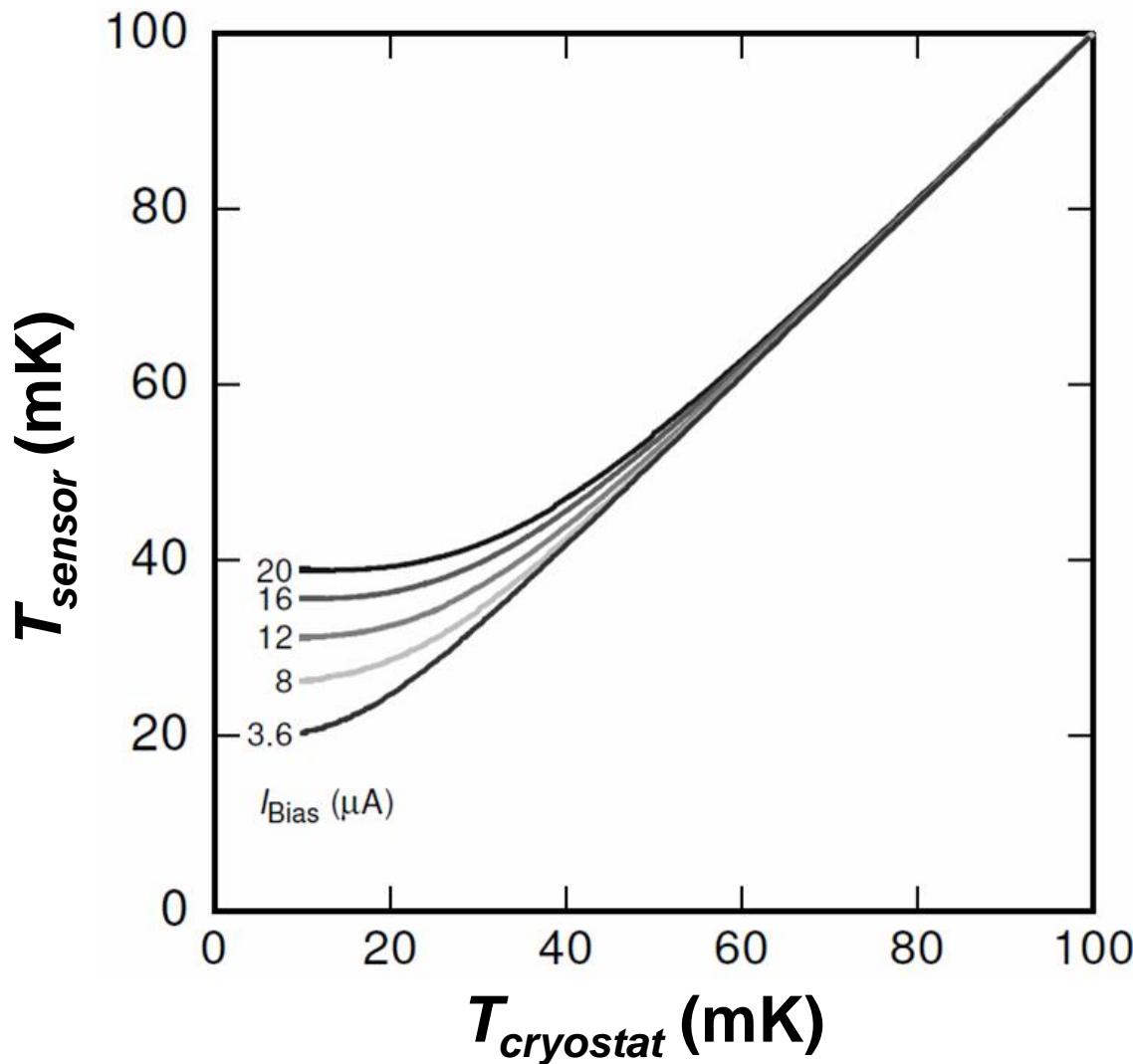
## Advantage

- High coupling factor
- Easy to realize

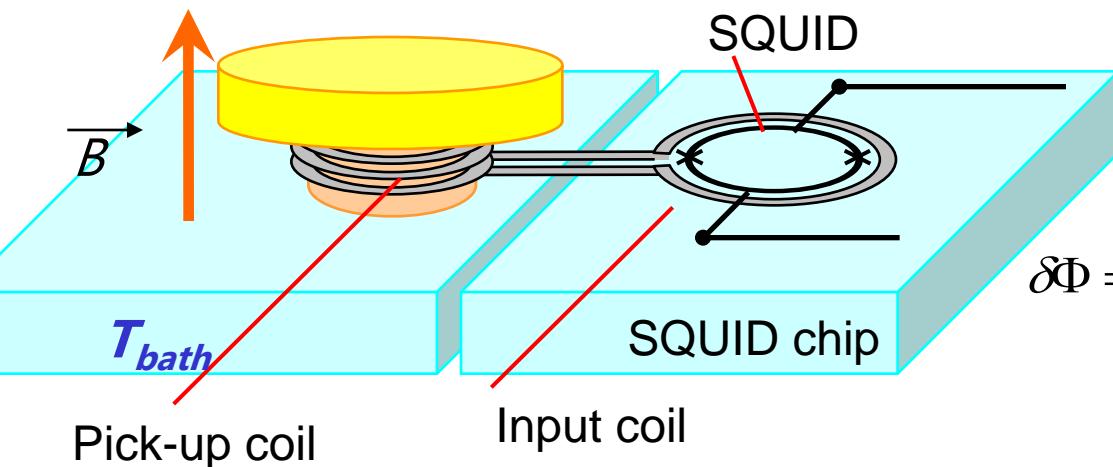
## Disadvantage

- Josephson junctions are sensitive to  $B$ 
  - Reduce the signal to noise ratio of the SQUID
- Thermal decoupling between bath and SQUID chip
- Sensor size and SQUID noise limited by SQUID loop radius
- Sensitive to magnetic Johnson noise

$$\sqrt{S_{\Phi,SQUID}} \propto L_{SQUID}^{3/4} \propto r_{SQUID}^{3/4}$$



# Flux transformer



$$\delta\Phi = \frac{G_{mag} G_{in}}{r_{pick-up}} \cdot V_s \cdot \mu_0 \cdot \left( \frac{\partial M}{\partial T} \right) \frac{E}{C_{sens} + C_{abs}}$$

Pick-up coil      Input coil

$$G_{in} = N_{turn} \frac{M_{in-SQ}}{L_{pick-up} + L_{input} + L_w}$$

Optimised for

$$L_{pick-up} = L_{input}$$

$$L_w \rightarrow 0$$

$$\sqrt{S_{\Phi, SQUID}^{pick-up}} \propto \sqrt{L_{pick-up}}$$

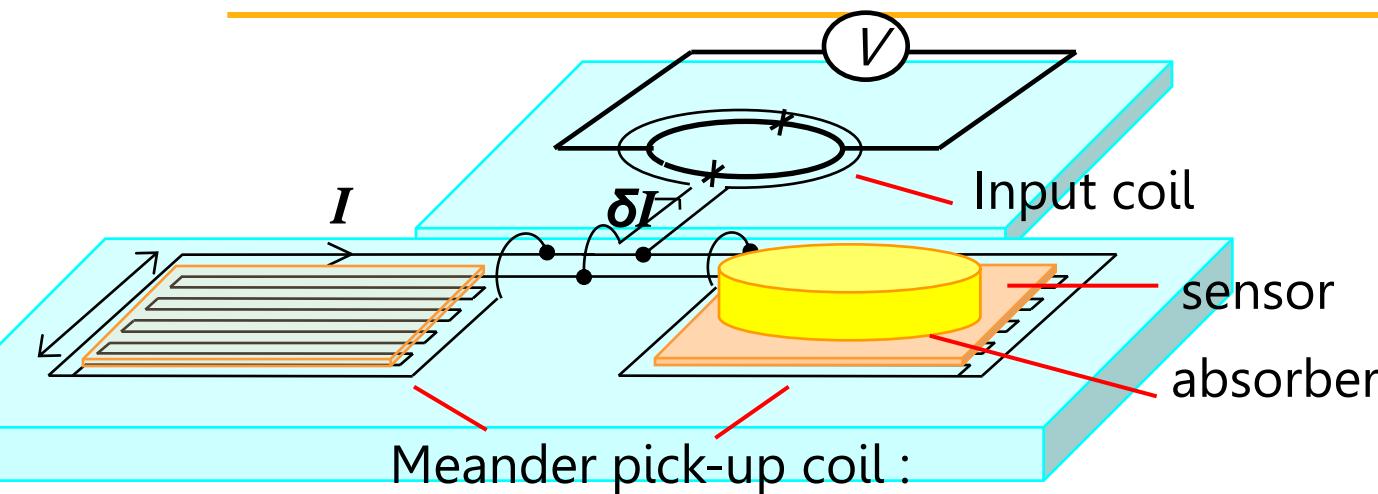
## Advantage

- Sensor thermally decouple from SQUID chip
- Possibility to read large sensor, required for applications needing a large absorber

## Disadvantage

- Signal to SQUID noise ratio is smaller by a factor 2 at least
- Sensitive to magnetic Johnson noise

# Flux transformer with meander shaped pickup coil

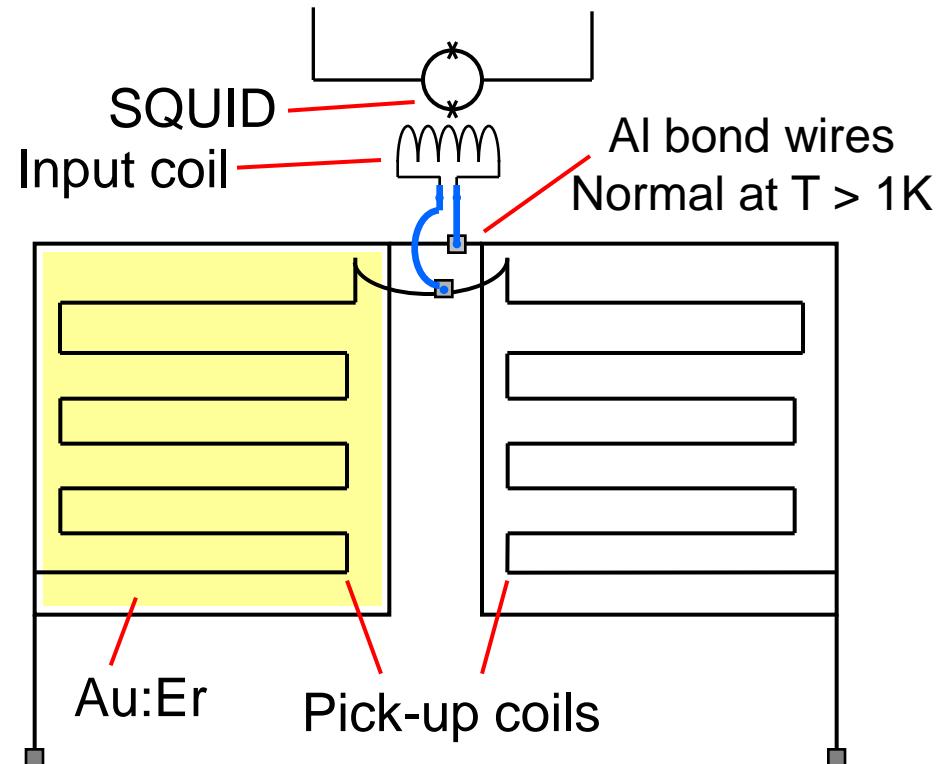


$$G_{in} = \frac{M_{in-SQ}}{2L_{meander} + L_{input}}$$

$$L_{meander} \propto \frac{A_{meander}}{p}$$

$G_{mag}$  ?

$B$  ?



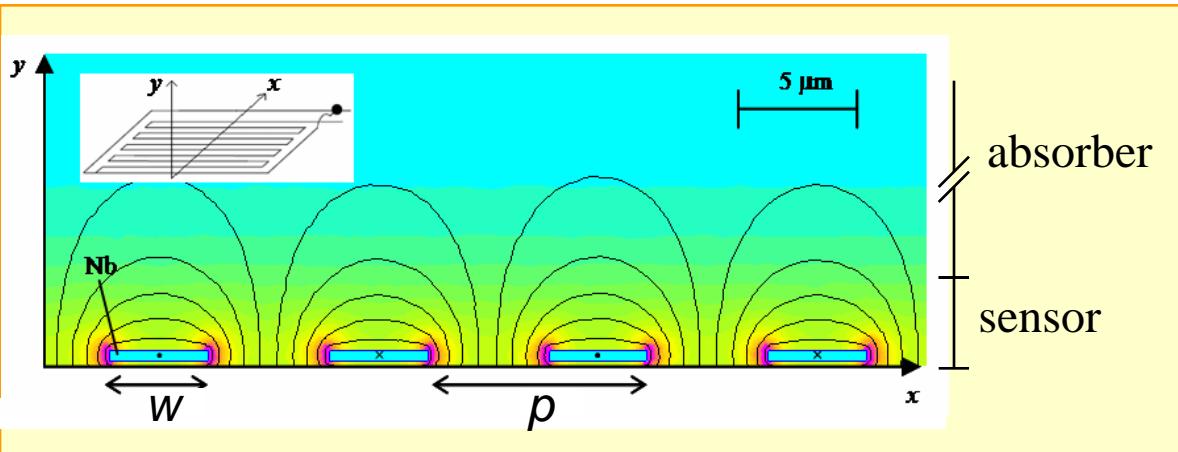
## Advantage

- Advantages of a flux transformer
- Insensitive to external magnetic field, Johnson magnetic noise
- No external field coil
- Gradiometric
- Microfabrication (reproducible, serial)

## Disadvantage

- Large current in the SQUID input coil
- Microfabrication (expensive equipments)
- Signal size reduced

# Field distribution

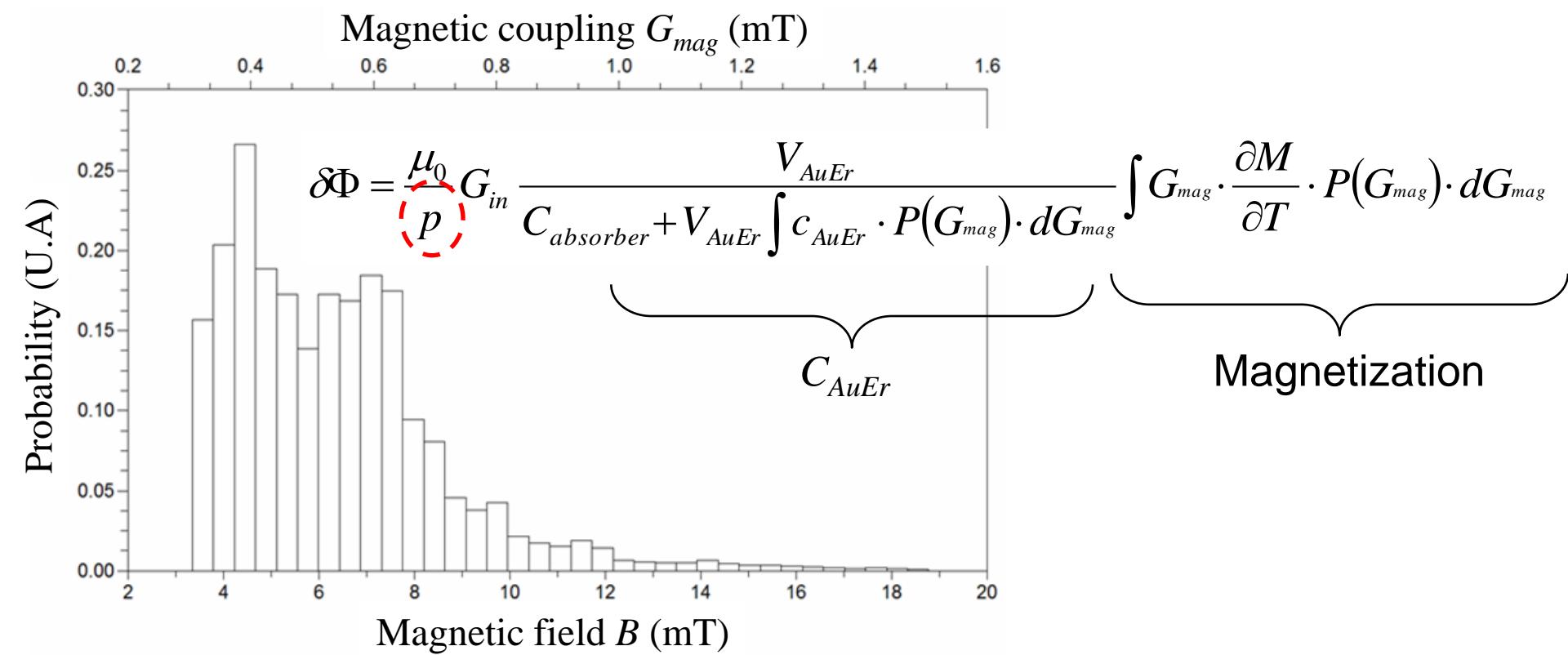


Inhomogeneous magnetic field  $B$

$$G_{mag} = Bp / \mu_0 I$$

$$w = 2 \dots 5 \mu\text{m}$$

$$p = 5 \dots 10 \mu\text{m}$$

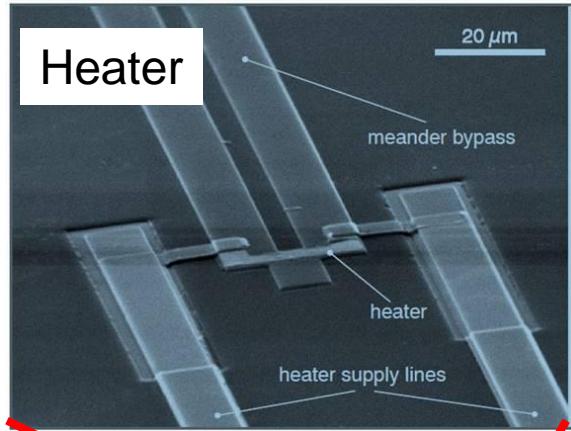


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# **Optimization, fabrication and experimental set-up**

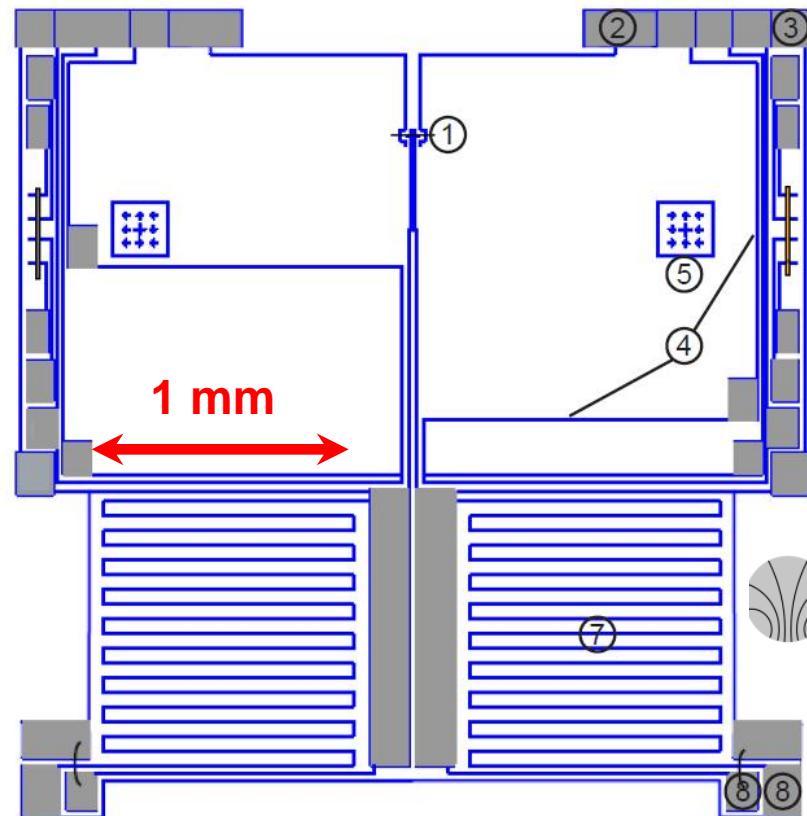
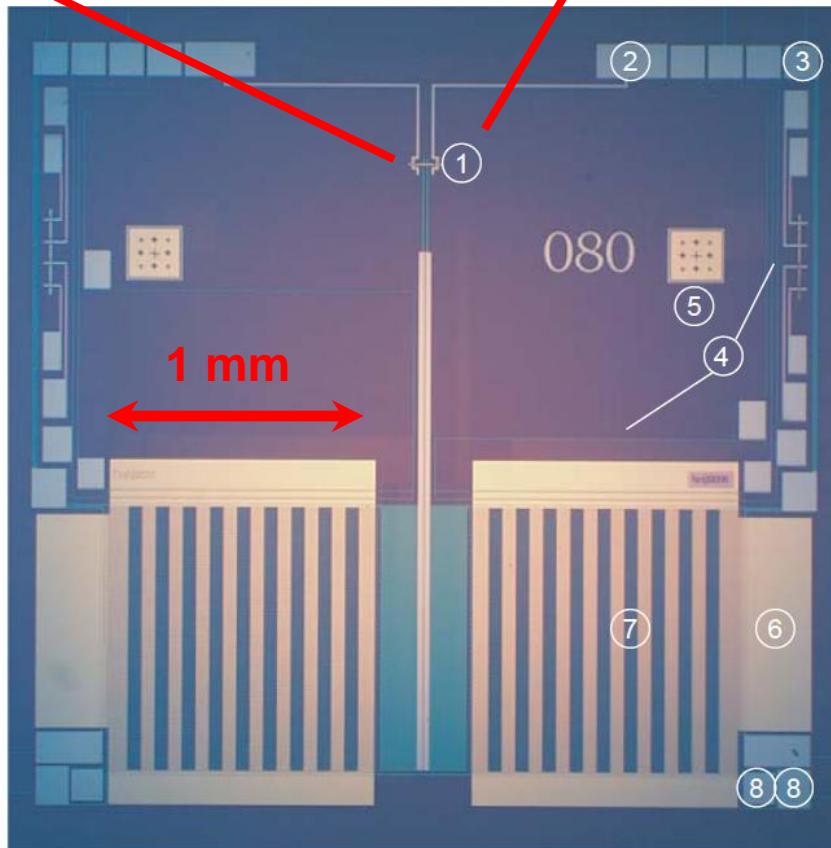
- $T_{bath}$  as low as possible but  $> 10 \text{ mK}$  and fixed by the cryostat
- $C_{absorber}$  as small as possible but fixed by the application
- Signal size as large as possible but  $< 1 \Phi_0$  in the SQUID loop
- $\tau_d$  as long as possible but limited by the count rate
- $B_{opt} \propto T_{bath}$
- $x_{opt} \propto T_{bath}$
- Signal  $\propto C_{absorber}^{1/3}$

# Meander shaped pick-up coil



Current of 100 mA required in the meander  
Good niobium film quality

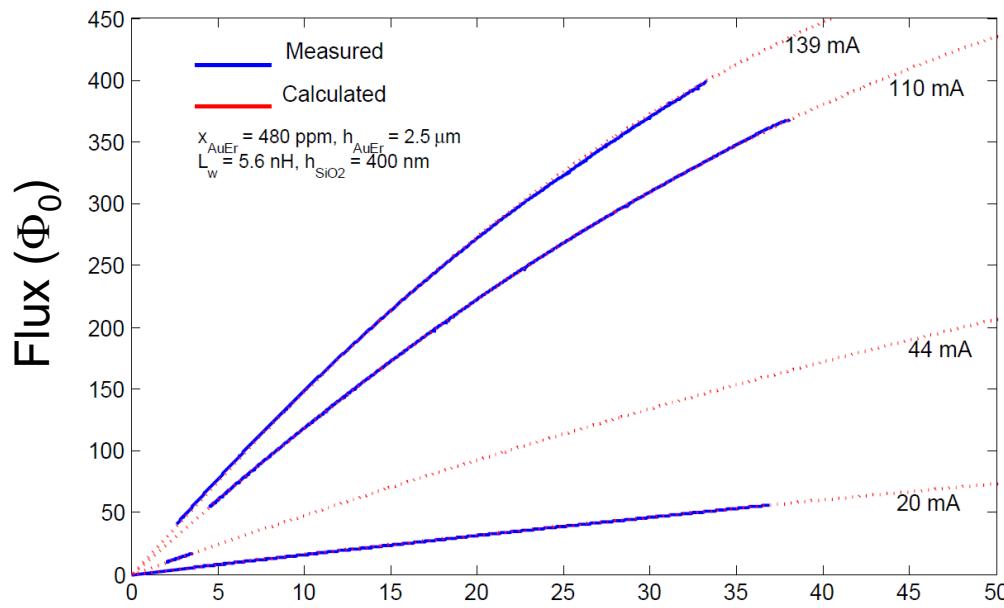
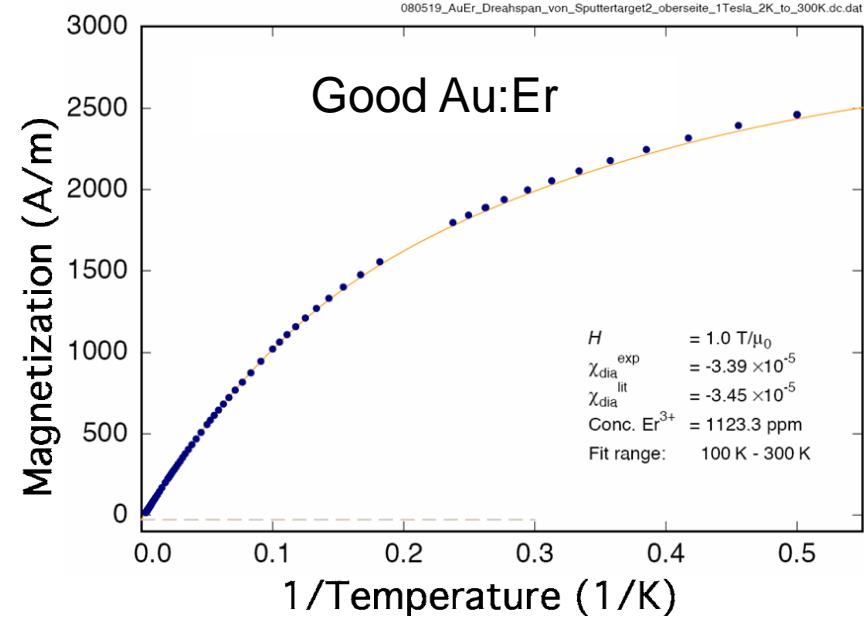
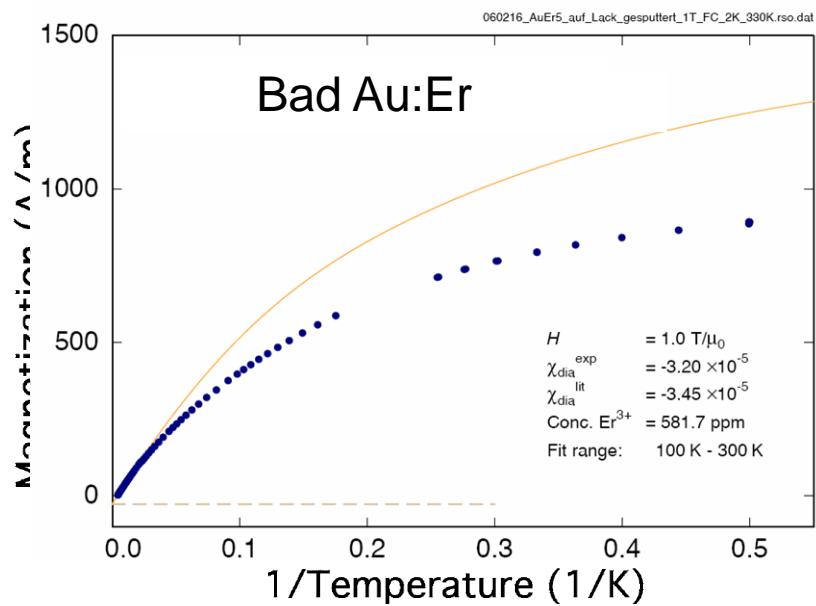
- 1 : Heater
- 2 : Heater bond pads
- 3 : Field bond pad
- 7 : Meander pick-up coil made of Nb
- 8 : SQUID input coil bond pads



# AuEr sensor

41

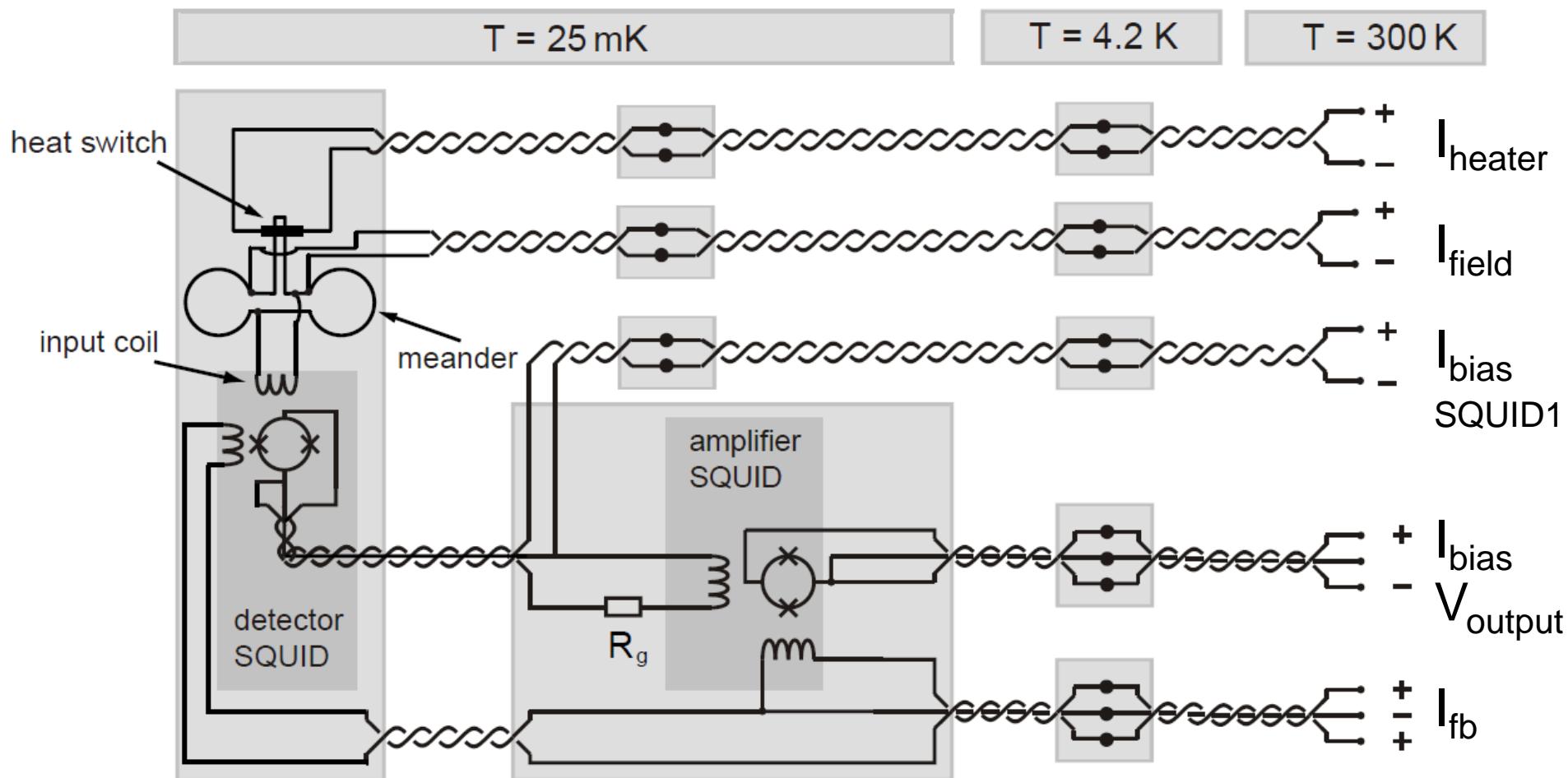
## Sputtering of the AuEr



← Good Au:Er at low T

UHV required <  $10^{-8} \text{ Torr}$

# Wiring

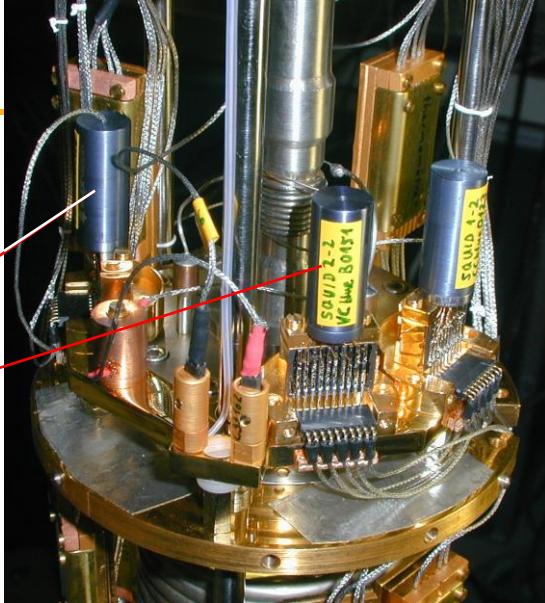


# In the cryostat

Dilution or ADR cryostat



SQUIDs of preamplification :  
 $T$  regulated between 1.5 and 4.2 K



Thermalisation of the wires and filters

Detector stages.  
Temperature regulation  
with a PID at 15 to 20 mK  $\pm$  few  $\mu\text{K}$





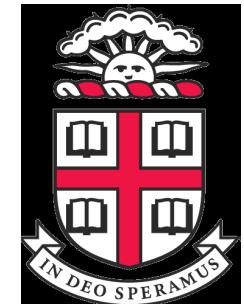
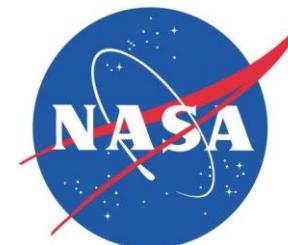
KIRCHHOFF  
INSTITUT  
FÜR PHYSIK



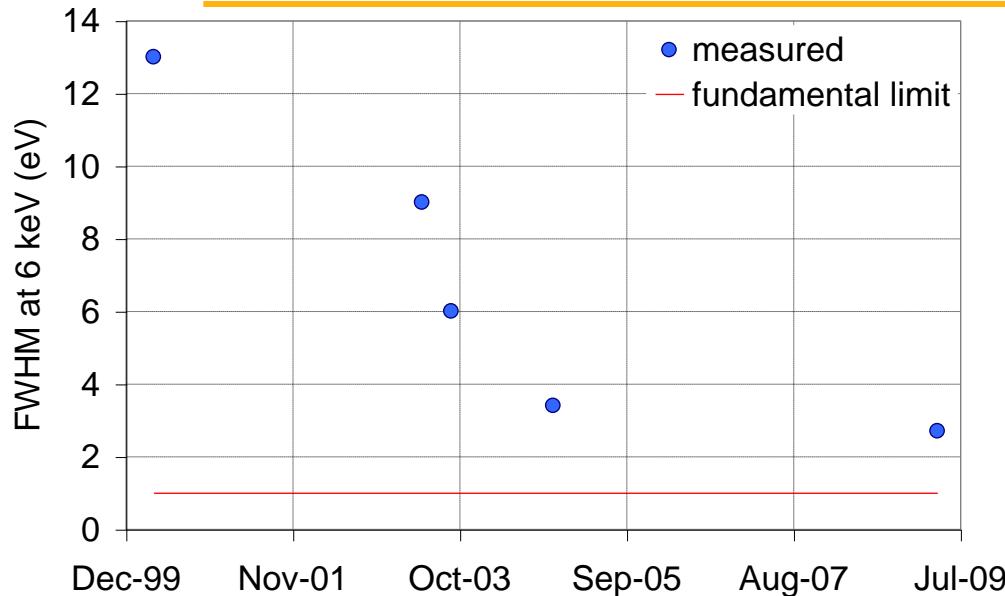
# Application External sources



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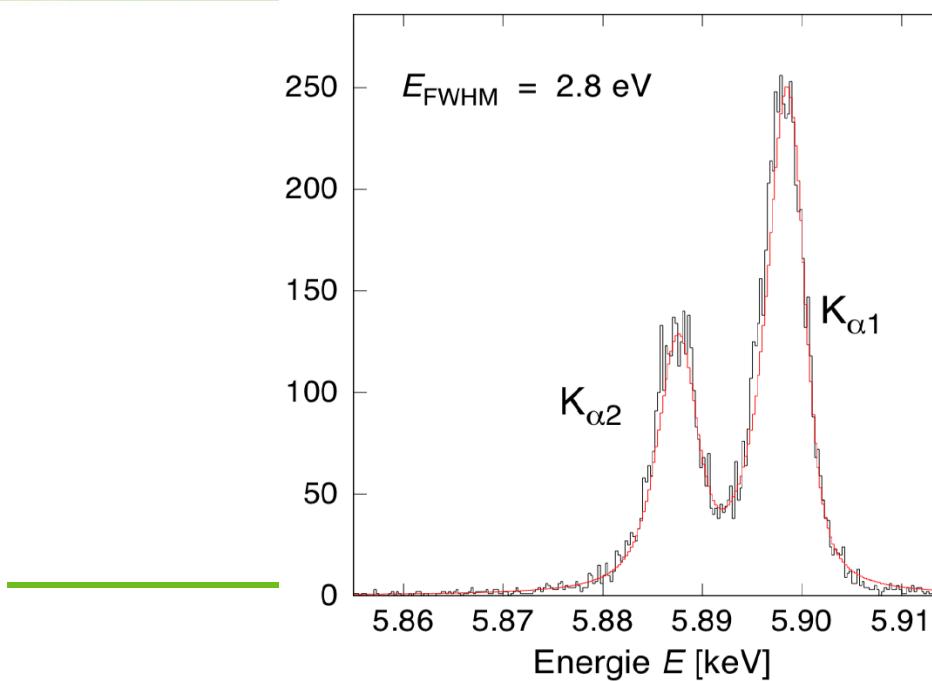
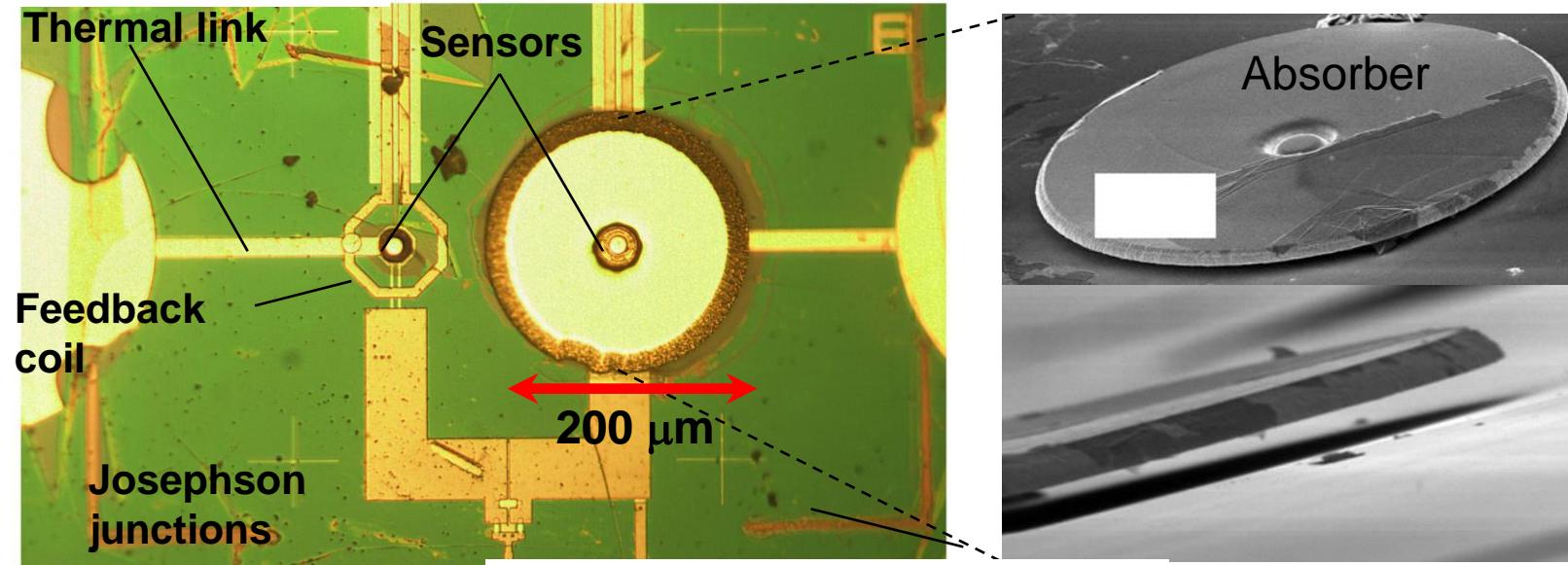


# X ray spectrometry



$T$	$C_{absorber}$ (pJ/K)	$C_{sensor}$ (pJ/K)	$\beta$	$B$ (mT)	$\delta\Phi/6 \text{ keV}$ ( $\Phi_0$ )	SQUID noise $\mu\Phi_0/\text{Hz}^{1/2}$	FWHM (eV)
30 mK	0.11	0.073	0.39	8	1.4	0.6	0.94
50 mK	0.19	0.067	0.26	12	0.65	0.6	2.2

Absorber:  $\pi \times 150 \times 150 \times 3 \text{ } \mu\text{m}^3$   $\rightarrow$  95 % detection efficiency at 6 keV

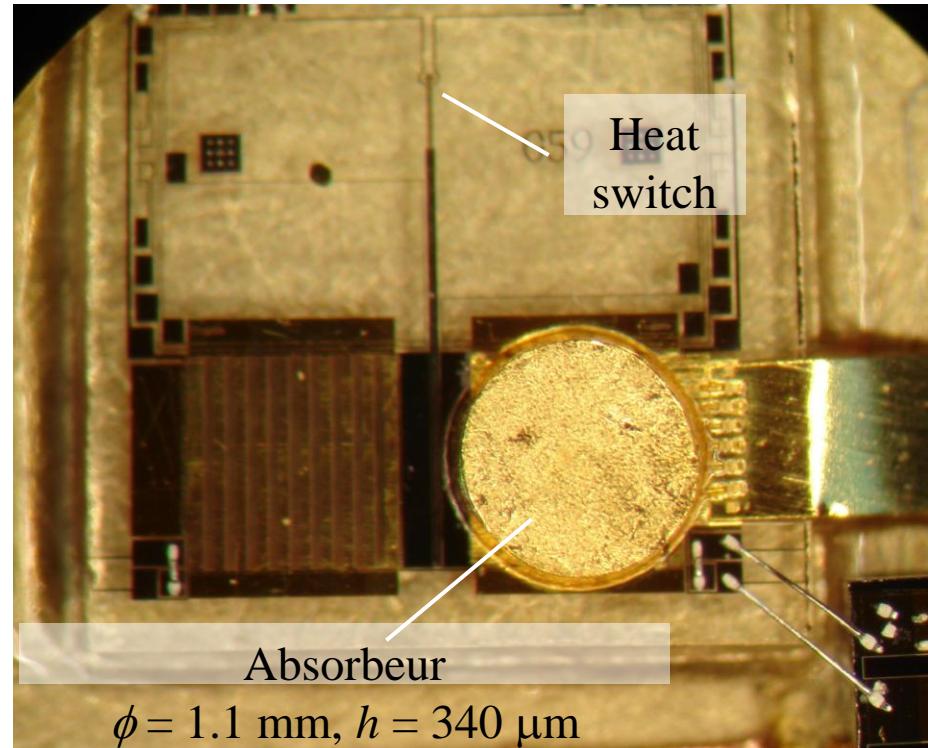
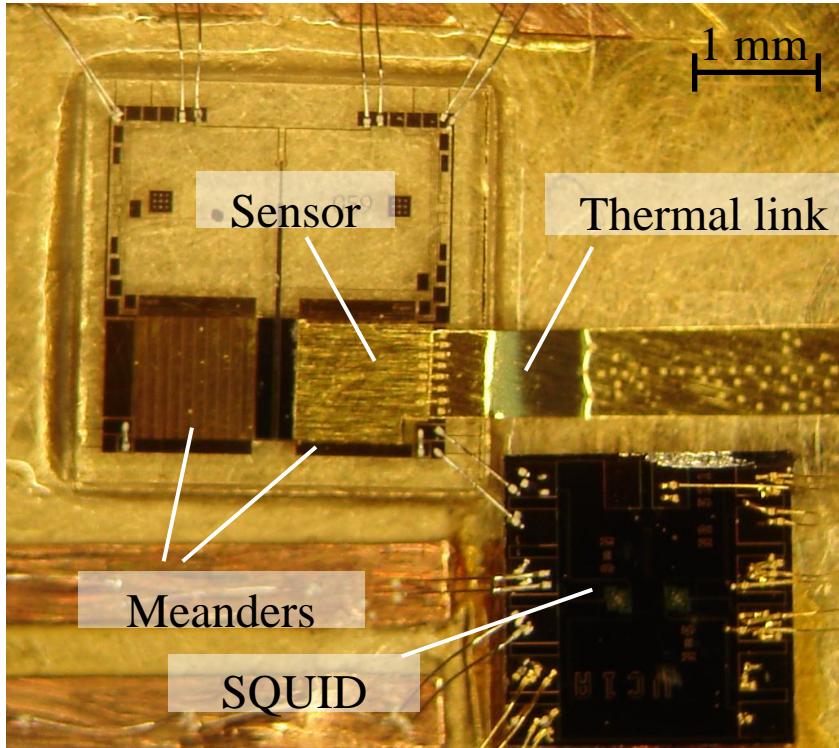




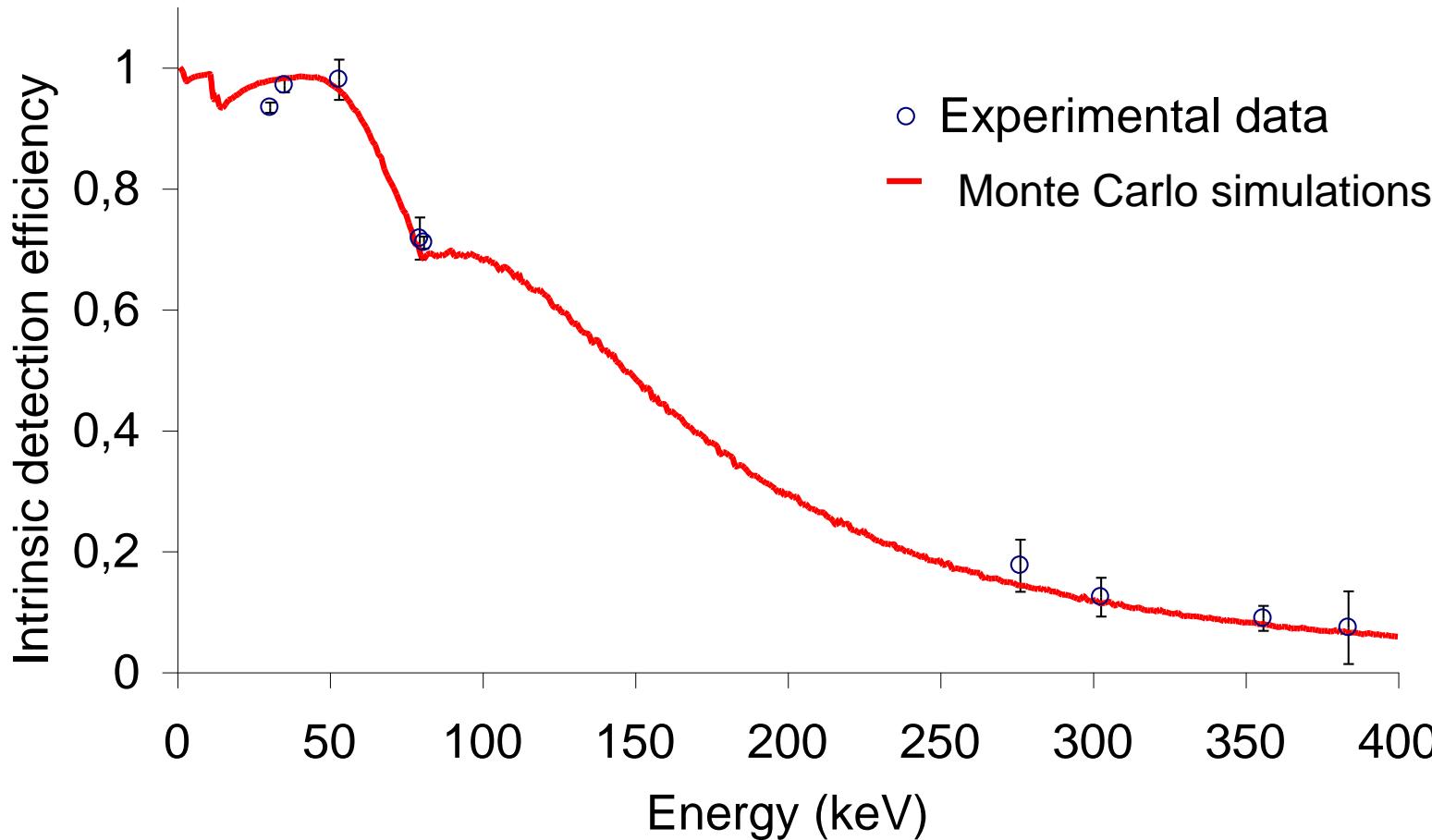
# Gamma spectrometry

$T$	$C_{absorber}$ (nJ/K)	$C_{sensor}$ (nJ/K)	$\beta$	$I$ (mA)	$\delta\Phi/100$ keV ( $\Phi_0$ )	SQUID noise $\mu\Phi_0/\text{Hz}^{1/2}$	FWHM (eV)
30 mK	0.5	0.41	0.45	80	0.17	0.5	45

Absorber:  $\pi \times 0.5 \times 0.5 \times 0.3 \text{ mm}^3$  60 % intrinsic detection efficiency at 100 keV



# Gamma spectrometry



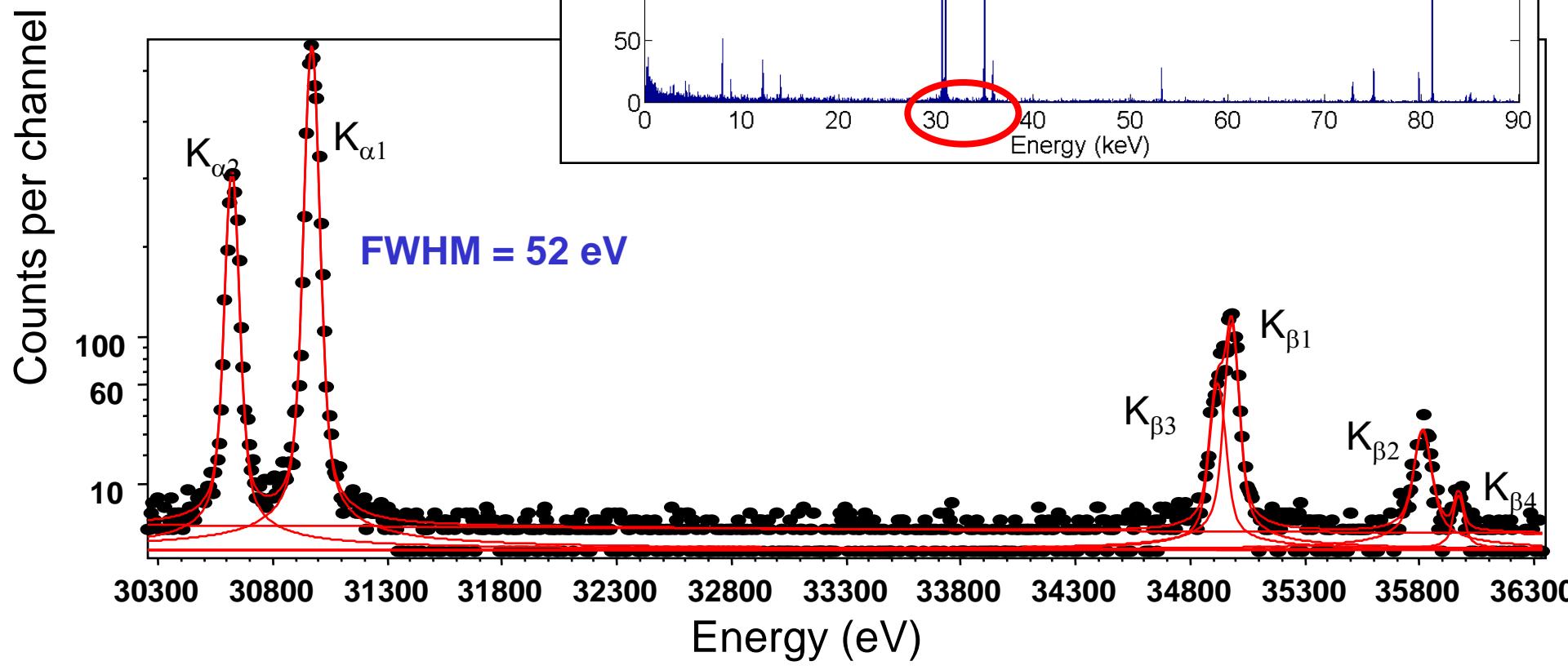


Le progrès, une passion à partager

**LNE**-cea

# Energy spectrum of a $^{133}\text{Ba}$ source

**FWHM of  
52 eV at 30 keV  
and 58 eV at 81 keV  
 $T = 13 \text{ mK}$**



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# Application Embedded sources

# Absolute activity measurement of $^{55}\text{Fe}$

51

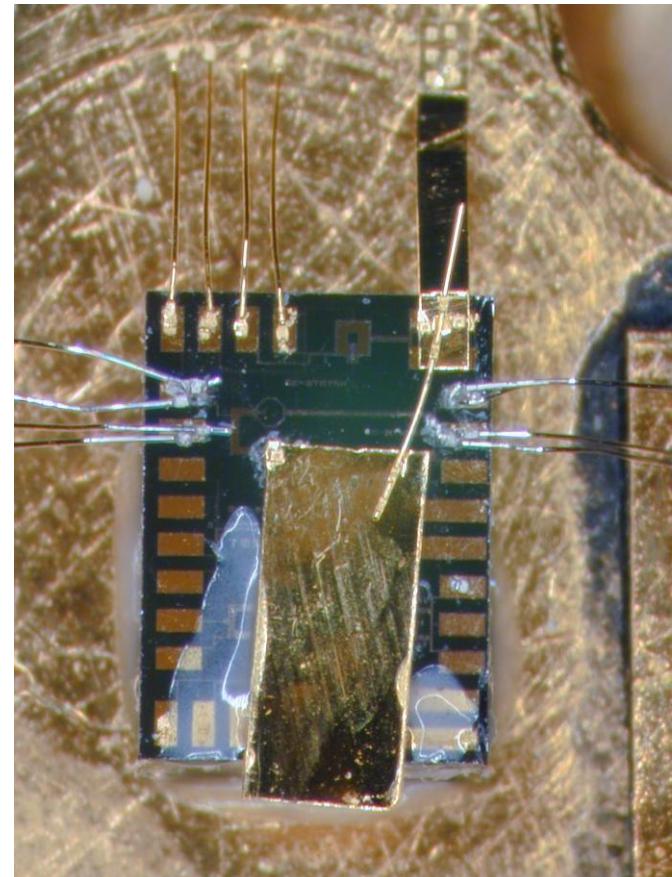
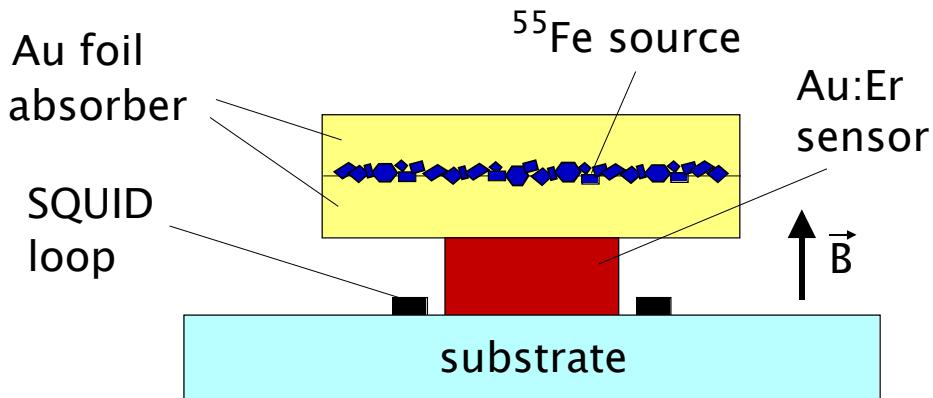


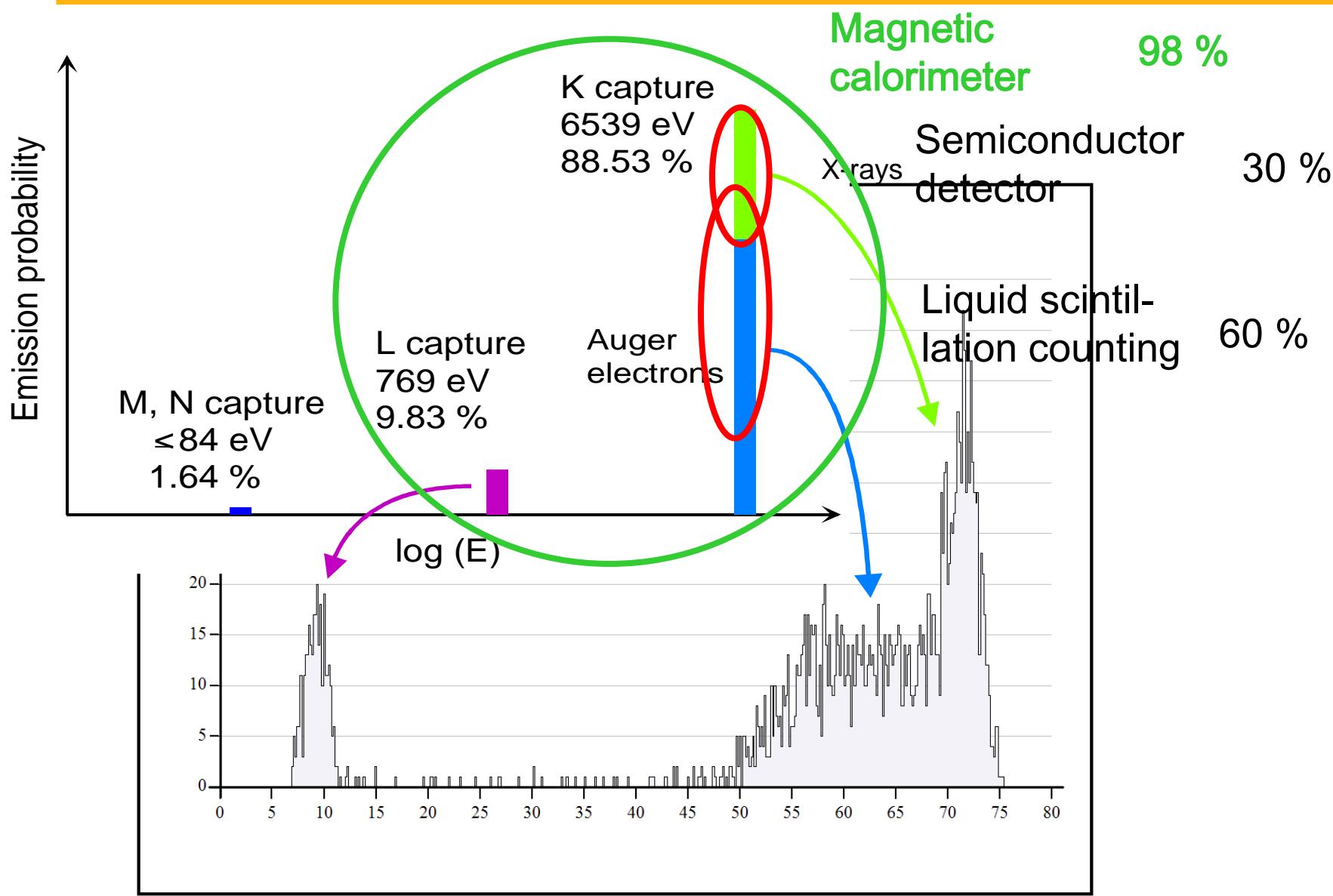
Source enclosed inside the absorber

→ 4 p detection geometry

Gold absorber: high stopping power  
thickness 12  $\mu\text{m}$ :  $\geq 99.9\%$  absorption  
for electrons and photons up to 6.5 keV

→ high detection efficiency





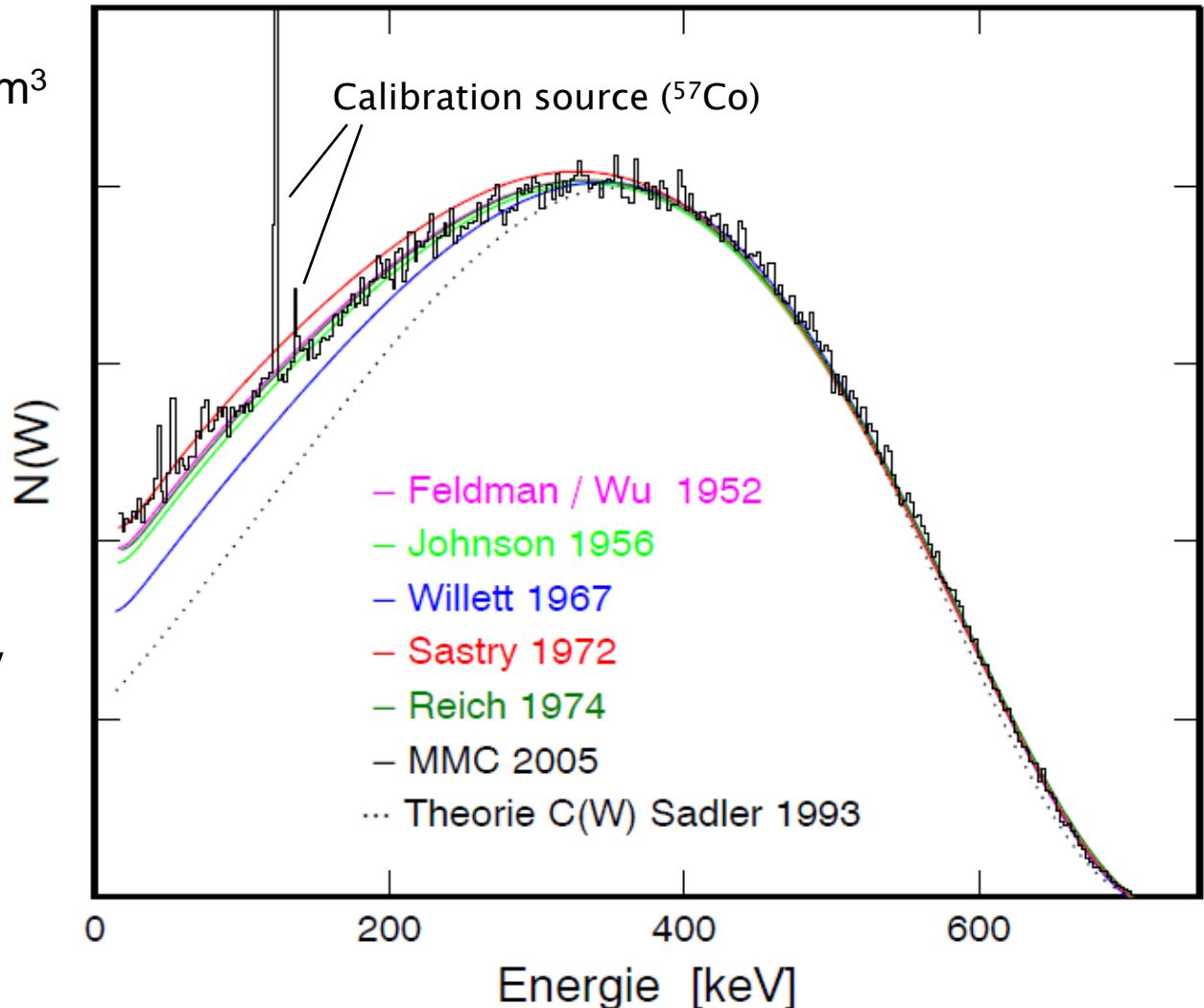


## Beta spectrometry

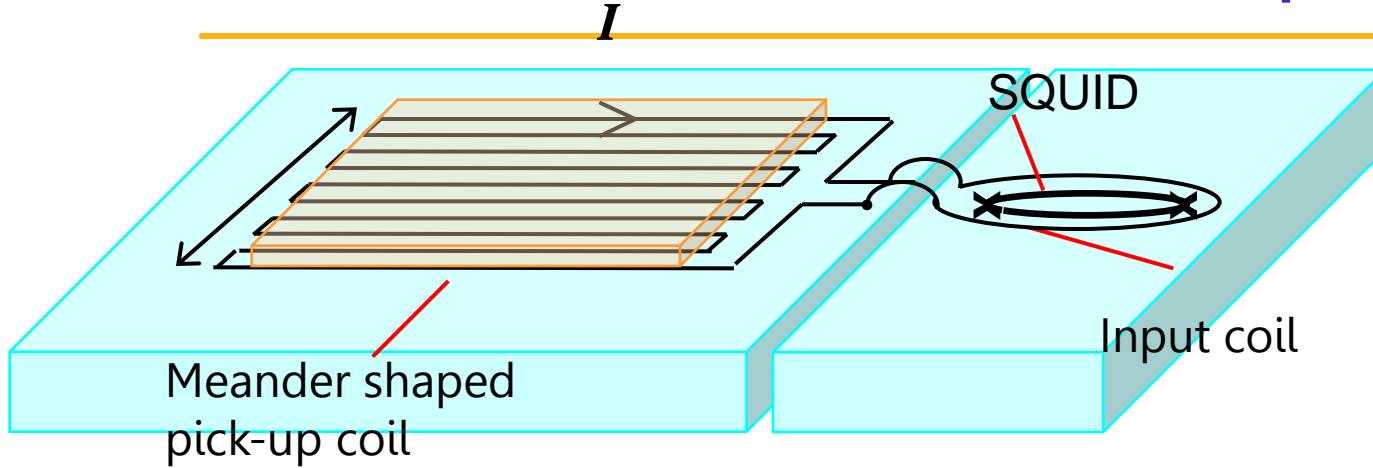
Using 1x1 mm<sup>2</sup> meander  
pick-up coil  
Absorber 800x800x500 μm<sup>3</sup>

750 000 counts  
(3.2 cps)

$\Delta E = 750 \text{ eV à } 122 \text{ keV}$



# Flux transformer with meander shaped pickup coil



$$G_{in} = \frac{M_{in-SQ}}{L_{meander} + L_{input}}$$

$$L_{meander} \propto \frac{A_{meander}}{p}$$

$G_{mag}$  ?

$B$  ?

## Advantage

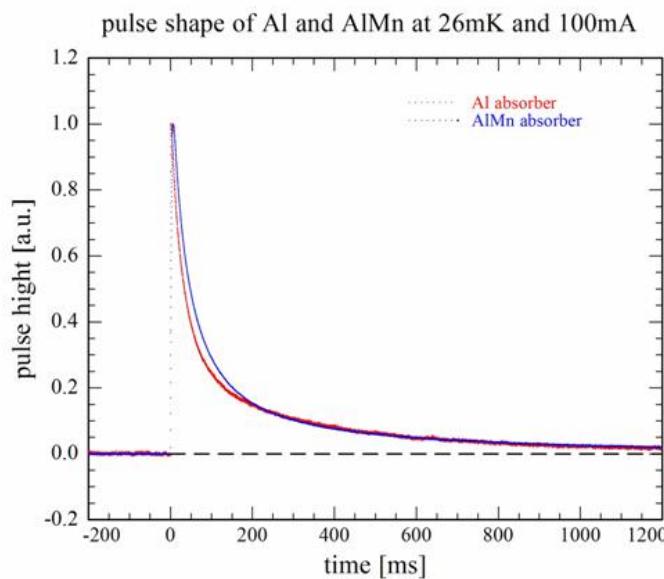
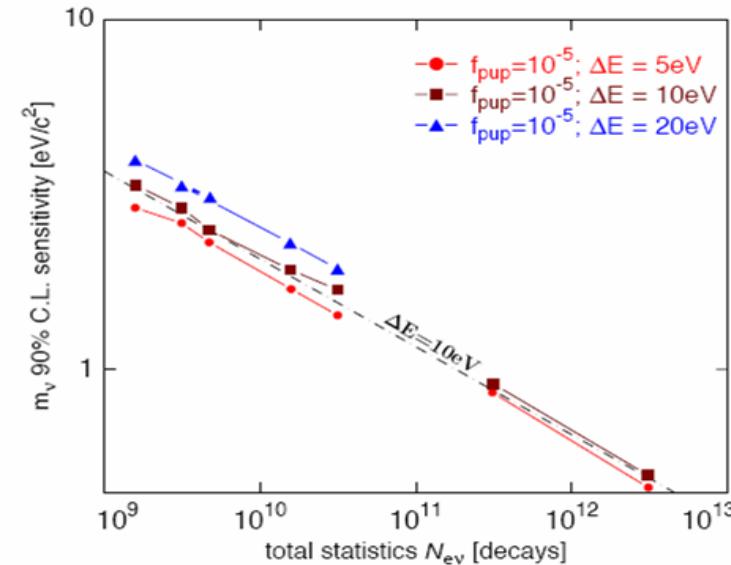
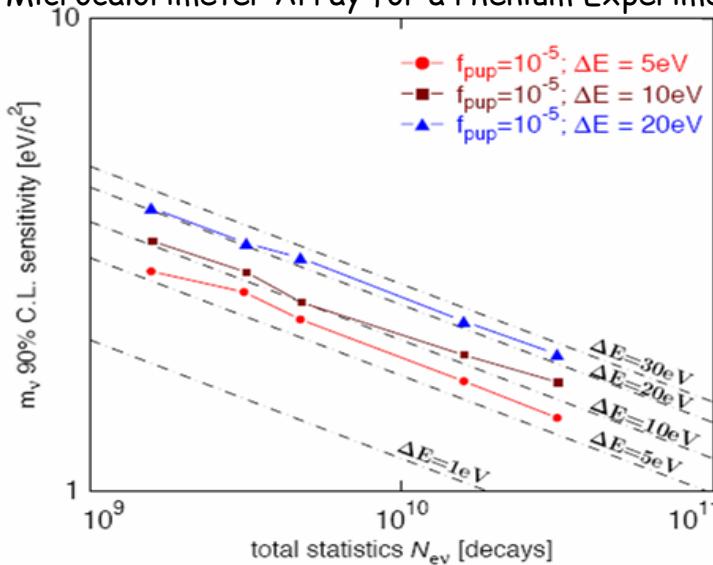
- Advantages of a flux transformer
- No external field coil
- Insensitive to external magnetic field, Johnson magnetic noise
- Microfabrication of arrays

## Disadvantage

- Large current in the SQUID input coil
- Microfabrication

# MARE project, neutrino mass

MARE Microcalorimeter Array for a rhenium Experiment



Superconducting absorbers



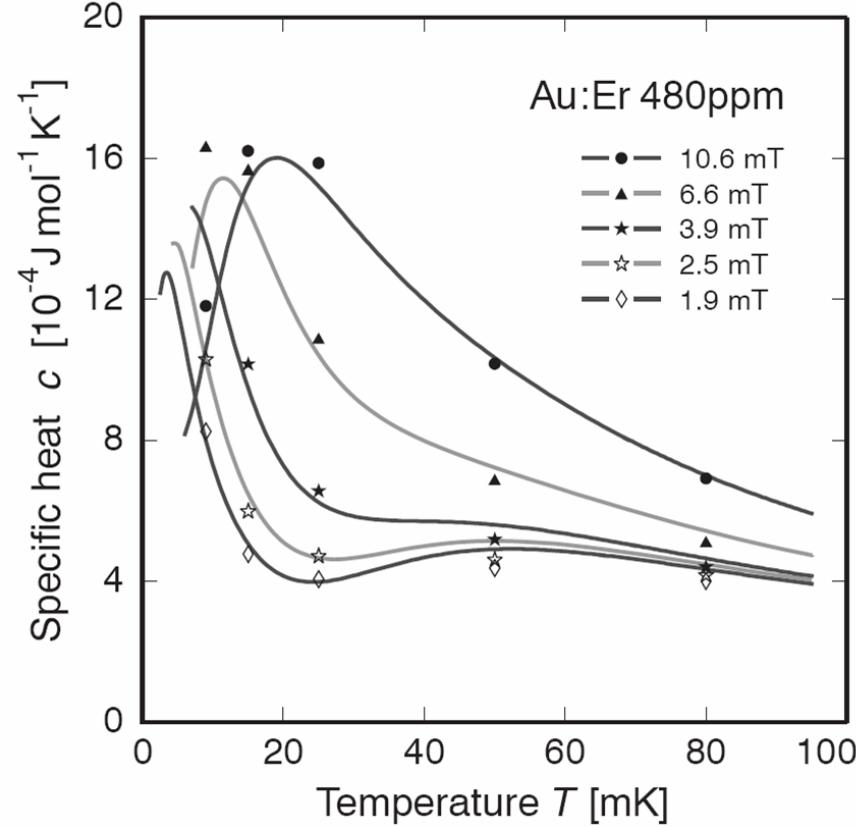
KIRCHHOFF  
INSTITUT  
FÜR PHYSIK

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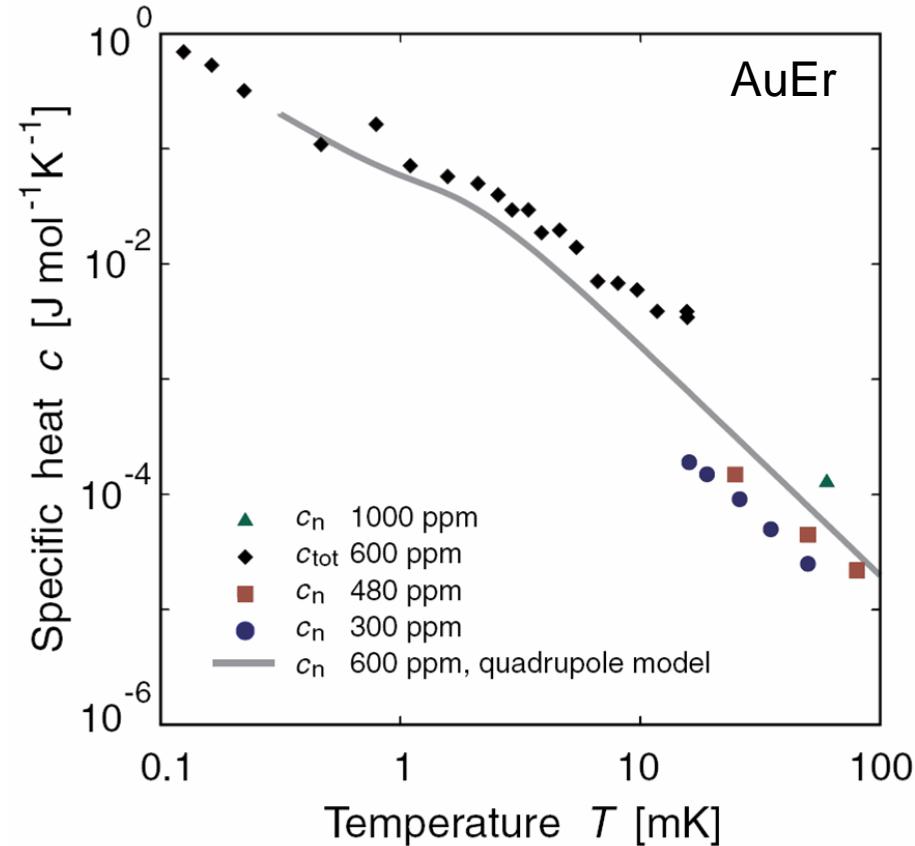
# Thank you for attention

$C_{add}'$  (hyperfine interactions between the nuclear magnetic moments of  $\text{Er}^{168}$ )

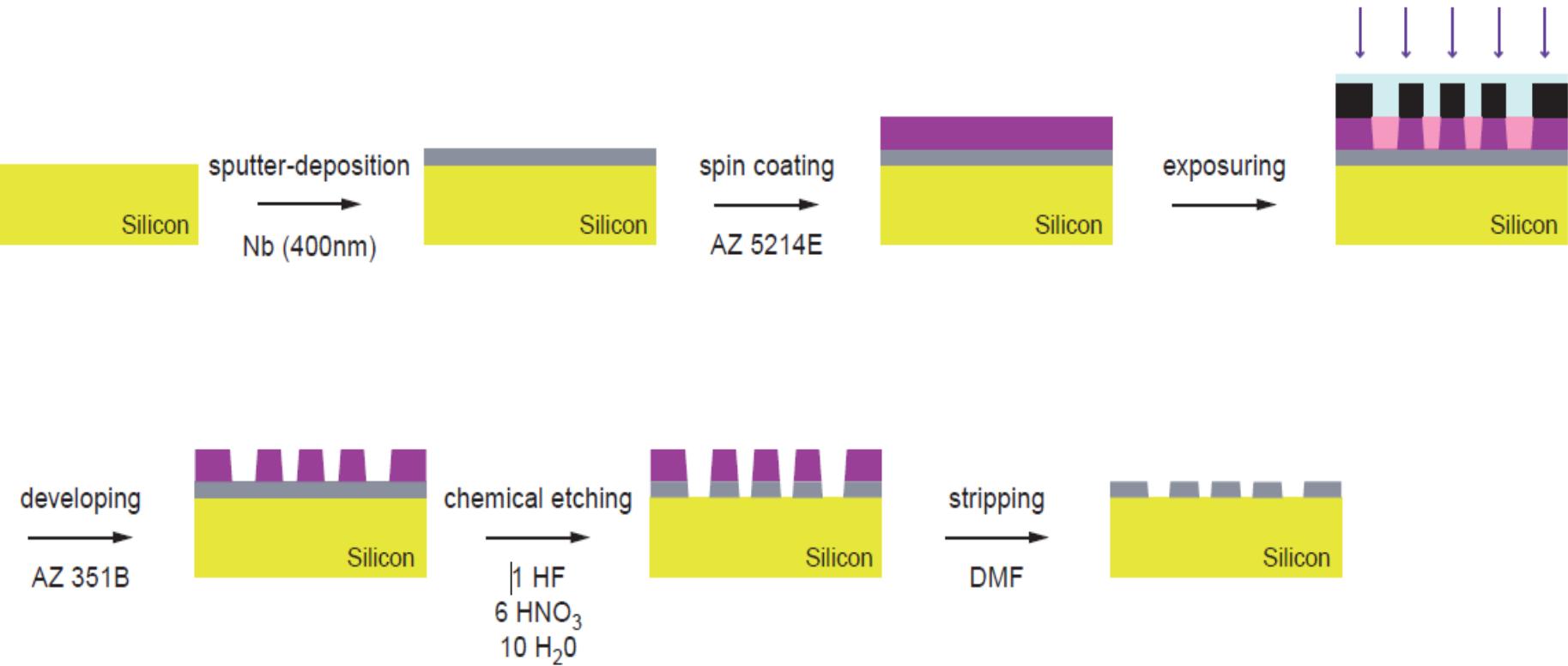
$I = 7/2$



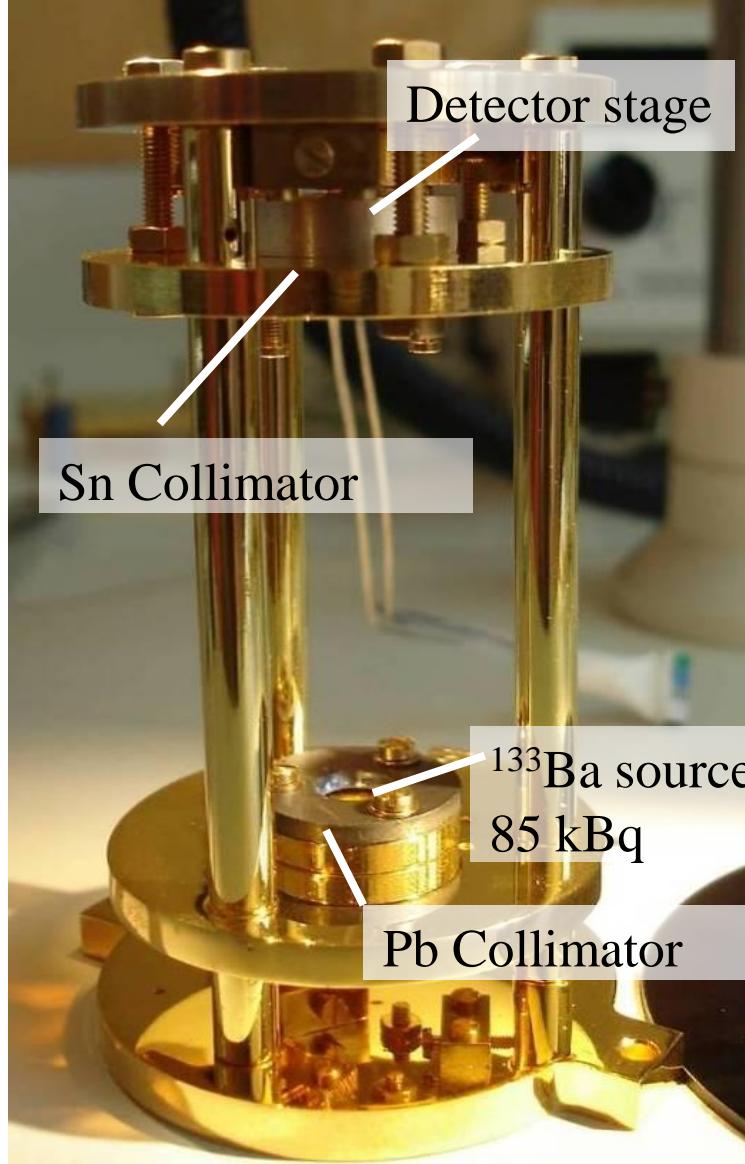
$C_{add}$  (interaction between the quadrupole moments of gold and the electric field gradient due to the presence of  $\text{Er}^{3+}$ )



AgEr could be a better choice below 20 mK even if the RKKY interaction is stronger than for

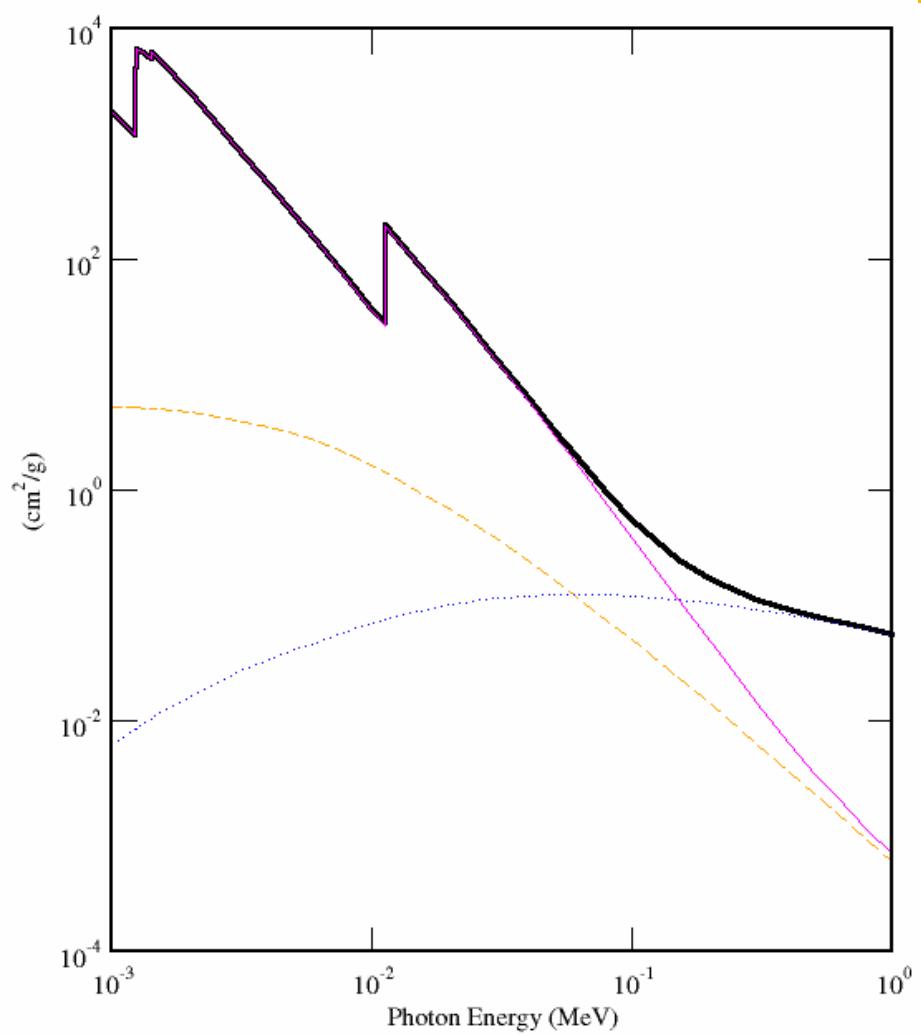


6 cm



The activity of the source  
was measured  
with a HPGe detector

# Germanium $Z = 32$



# Gold $Z = 79$

